



**SIGGRAPH** 2020 [2020.SIGGRAPH.ORG](https://2020.siggraph.org) **THINK BEYOND**

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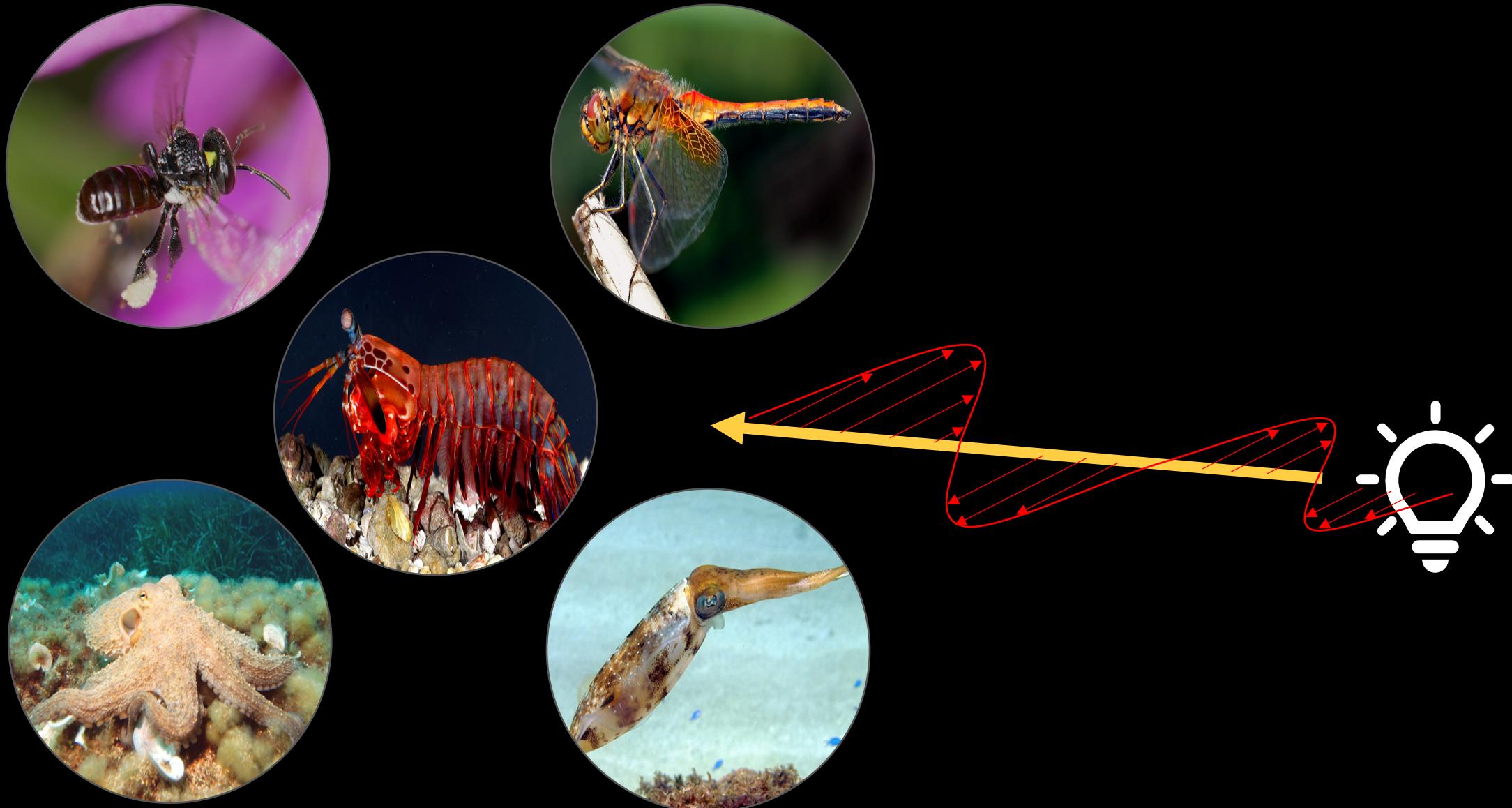
**IMAGE-BASED  
ACQUISITION AND MODELING  
OF POLARIMETRIC REFLECTANCE**

Seung-Hwan Baek, Tizian Zeltner, Hyun Jin Ku,  
Inseung Hwang, Xin Tong, Wenzel Jakob, Min H. Kim

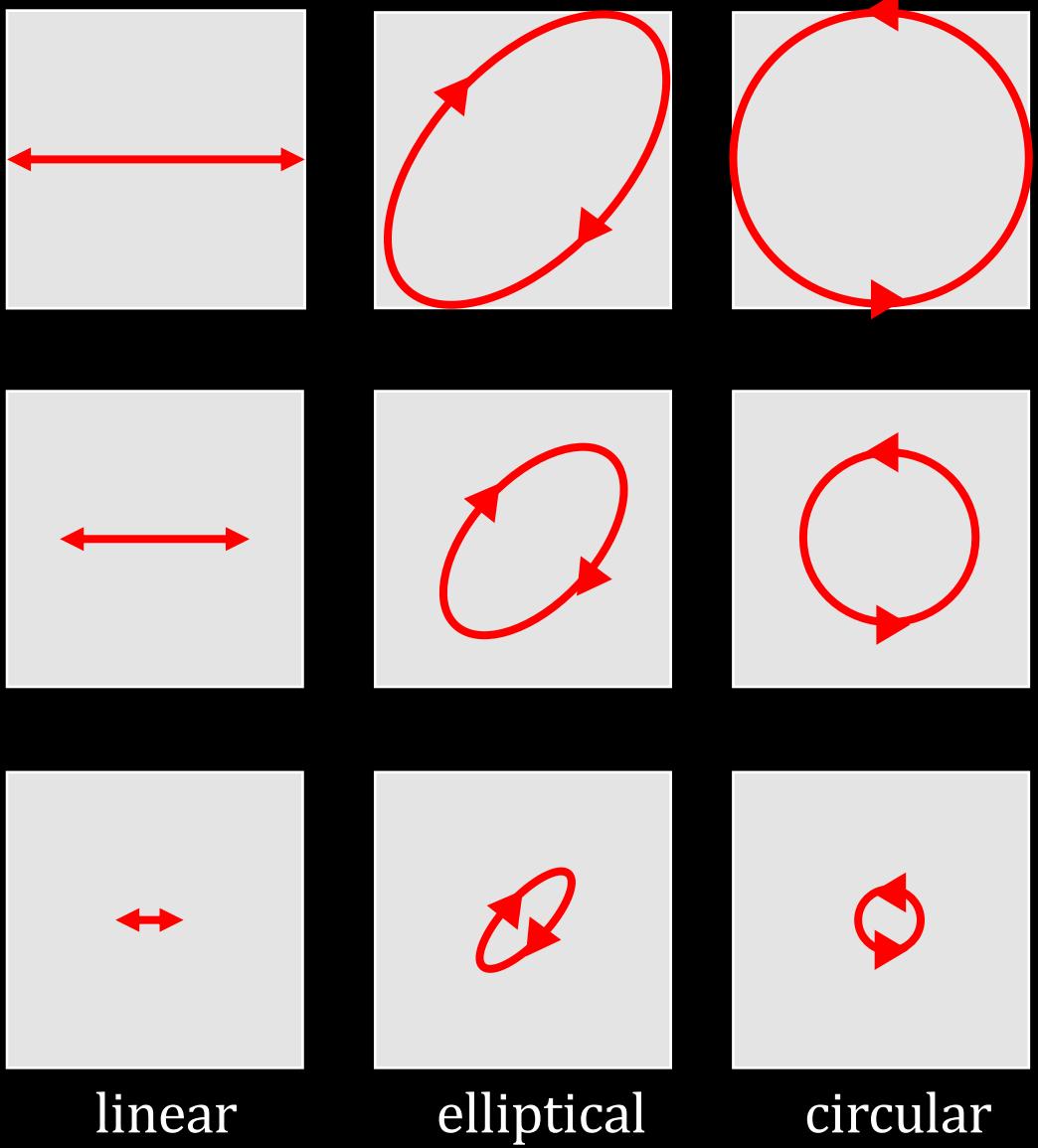
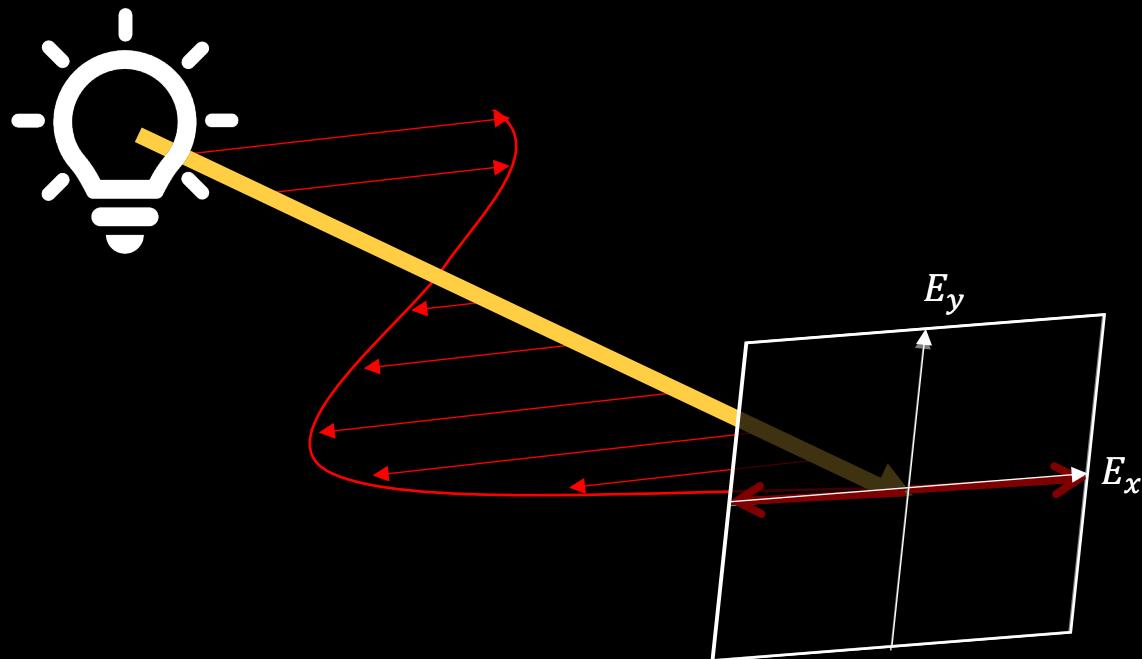
# Human vision senses light



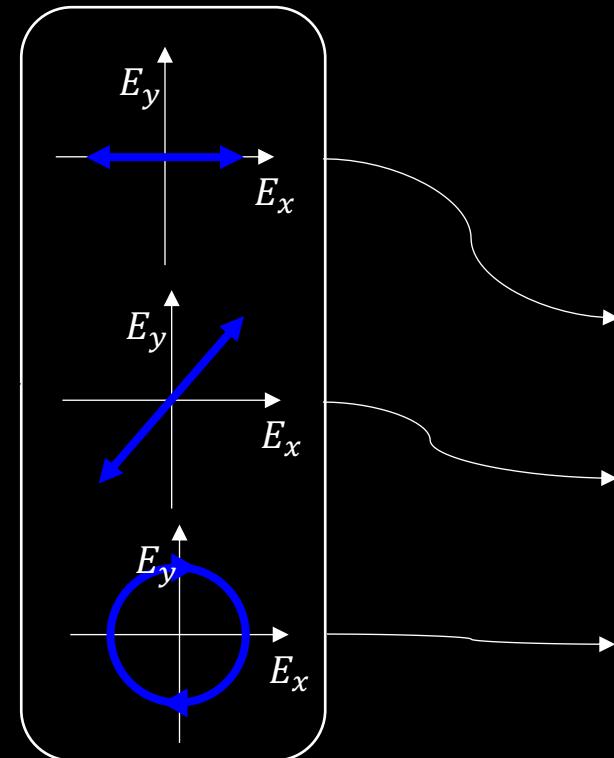
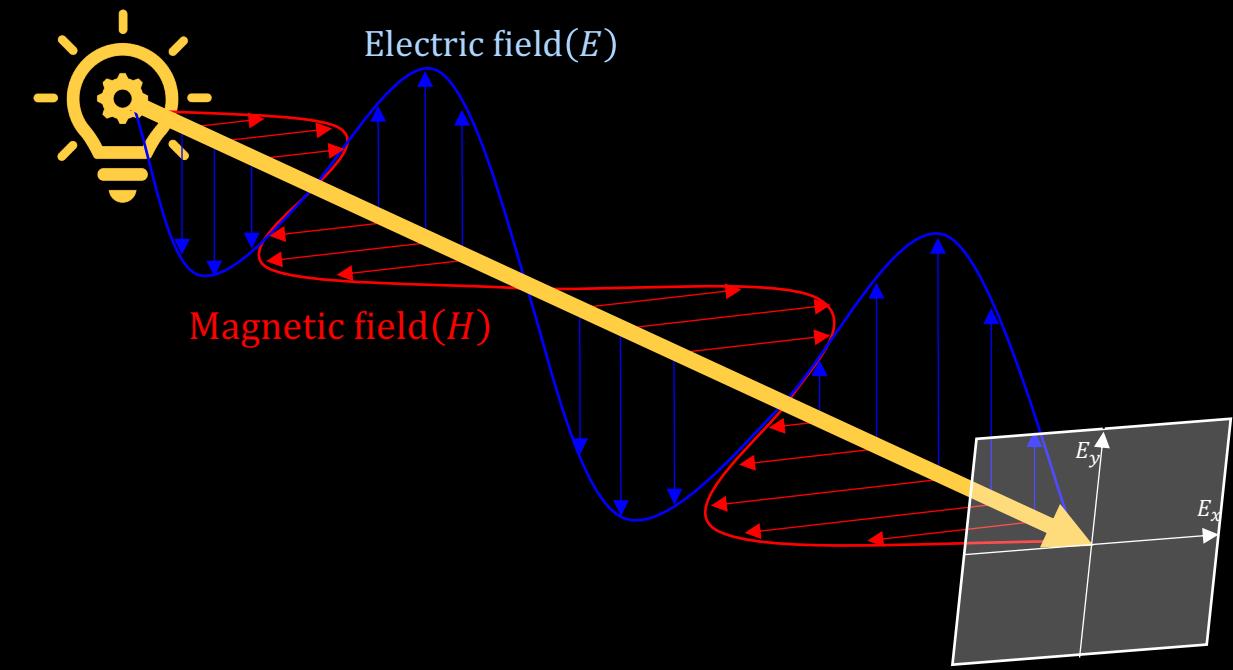
# Light “wave”



# Polarization



# Stokes Vector



$$\begin{bmatrix} S_0 \\ S_1 \\ S_2 \\ S_3 \end{bmatrix} \begin{array}{l} \text{Overall Intensity} \\ \text{0 degree} \\ \text{45 degree} \\ \text{Circular} \end{array}$$

Geometric orientation of  
the E-field's oscillation

# Mueller Matrix

$$\mathbf{M} = \begin{bmatrix} M_{00} & M_{01} & M_{02} & M_{03} \\ M_{10} & M_{11} & M_{12} & M_{13} \\ M_{20} & M_{21} & M_{22} & M_{23} \\ M_{30} & M_{31} & M_{32} & M_{33} \end{bmatrix}$$

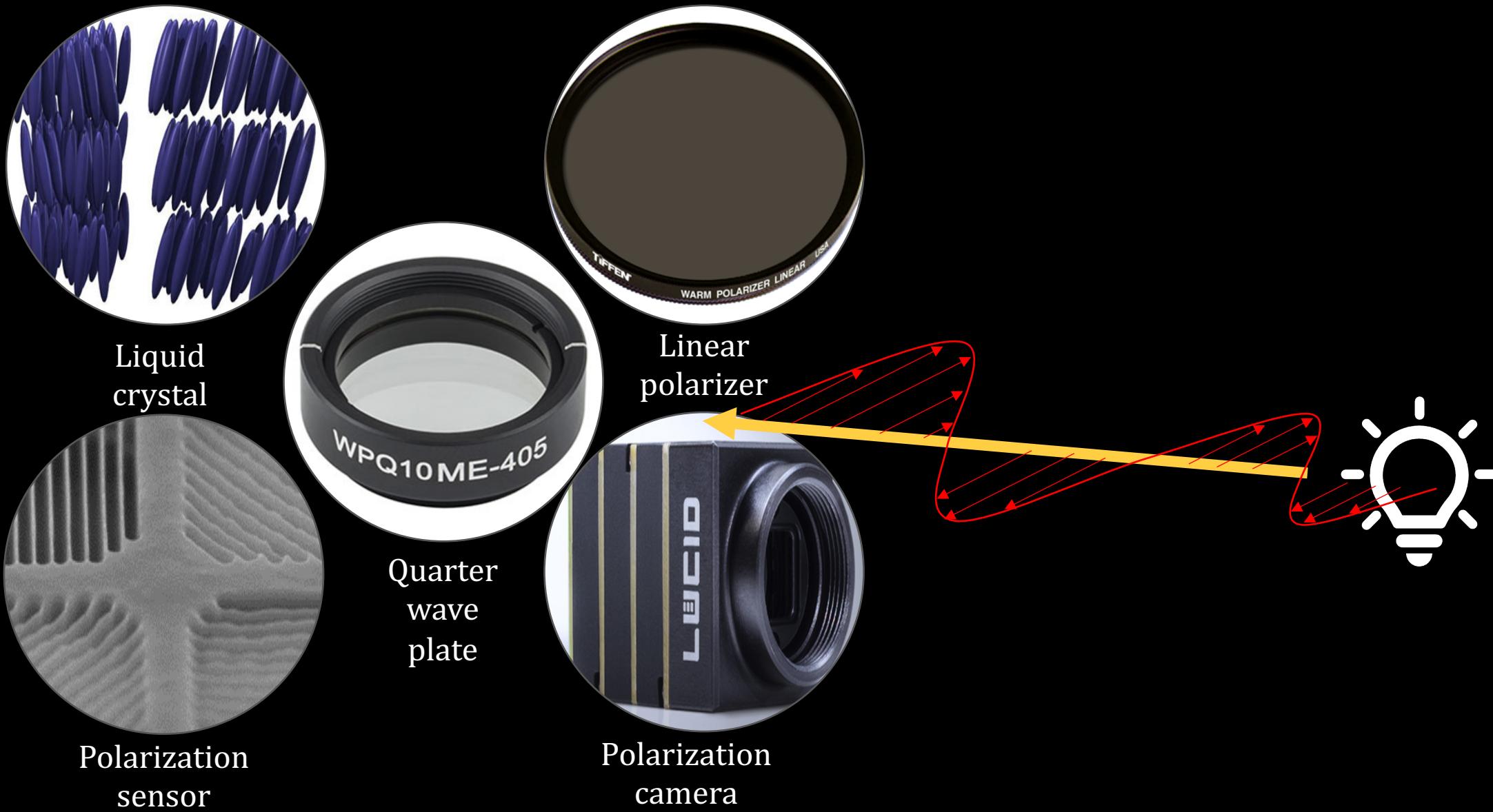
$\mathbf{s}_{\text{before}}$



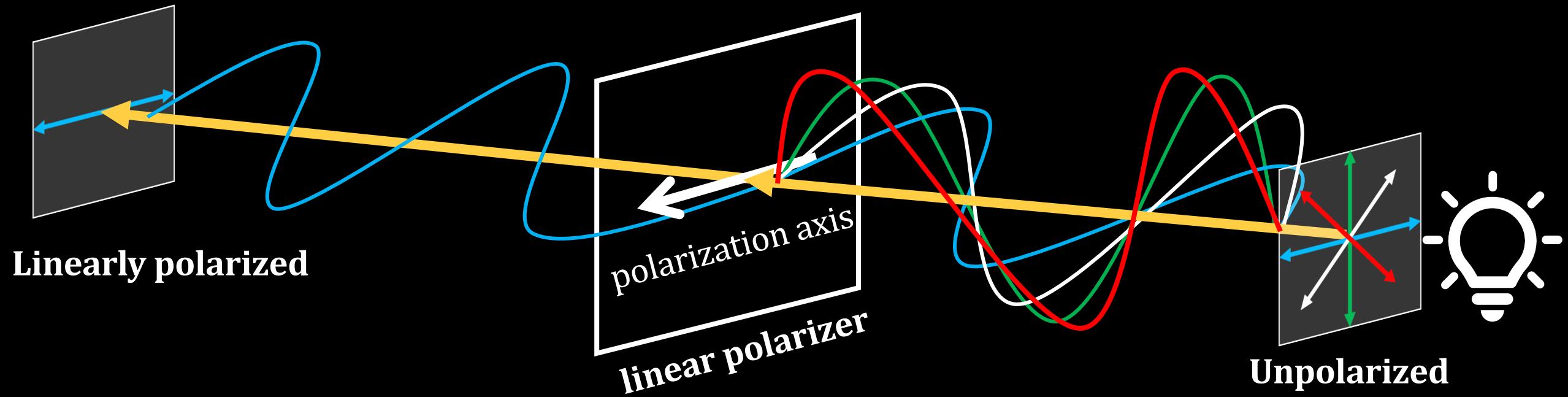
$\mathbf{s}_{\text{after}}$

$$\mathbf{s}_{\text{after}} = \mathbf{M}\mathbf{s}_{\text{before}}$$

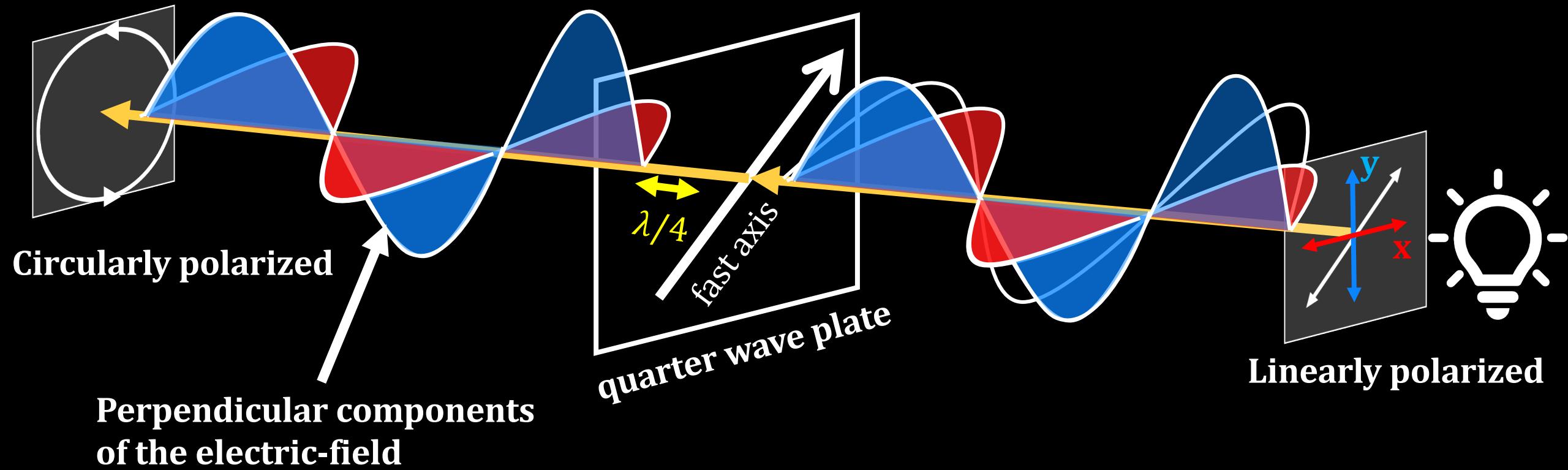
# Polarization imaging



# Linear polarizer

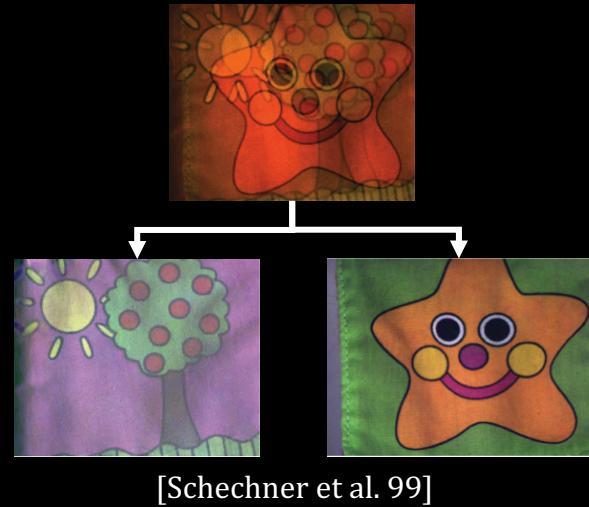


# Quarter wave plate

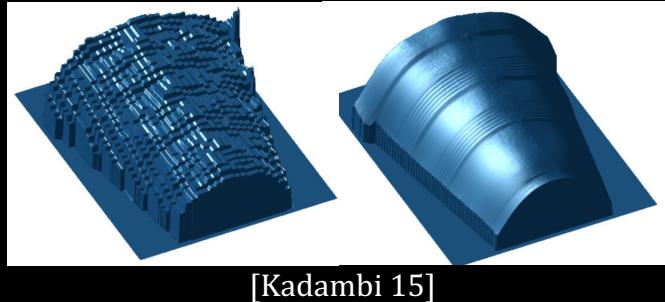


# Polarization imaging for scene analysis

## Reflection removal and descattering

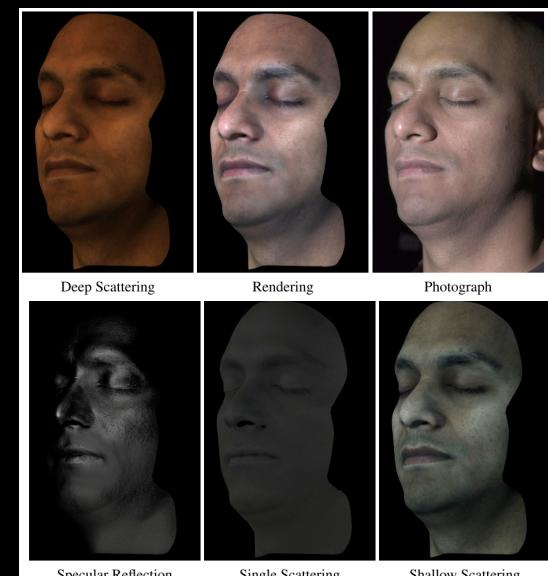
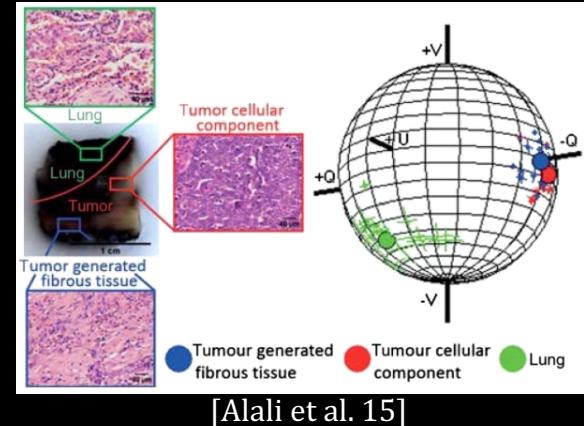


## Shape and appearance acquisition



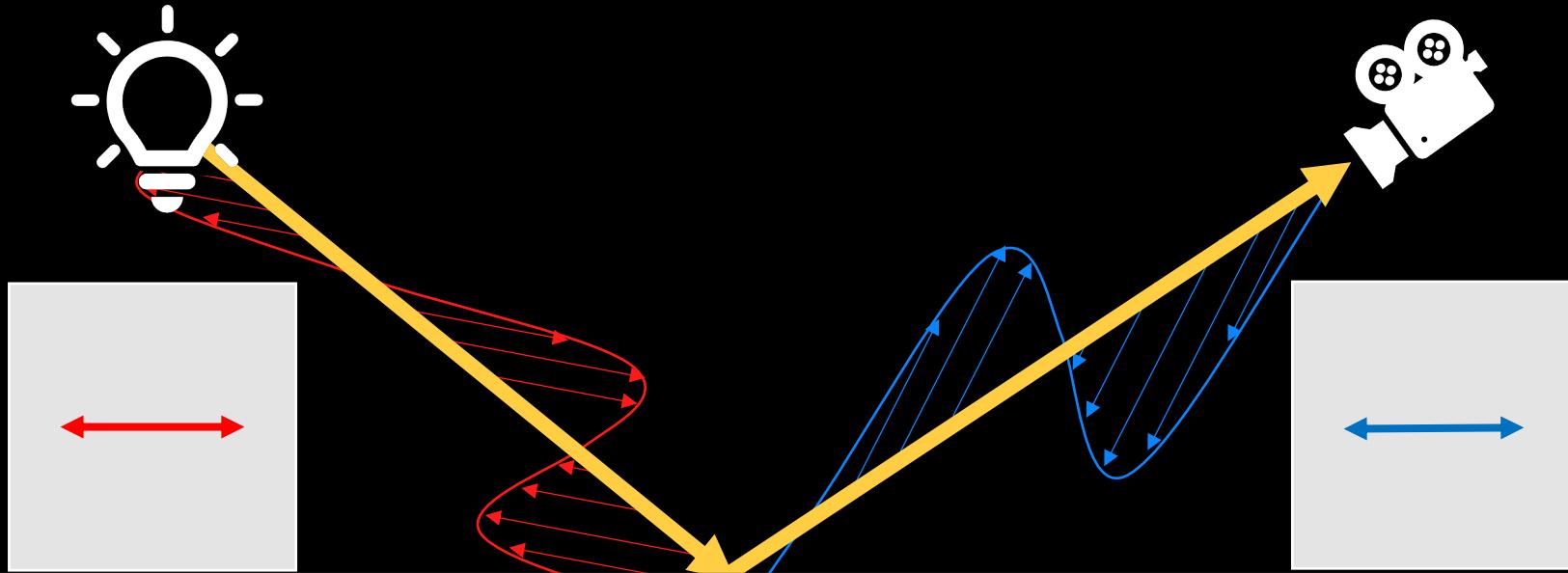
[Baek et al. 18]

## Segmentation



[Ghosh et al. 08]

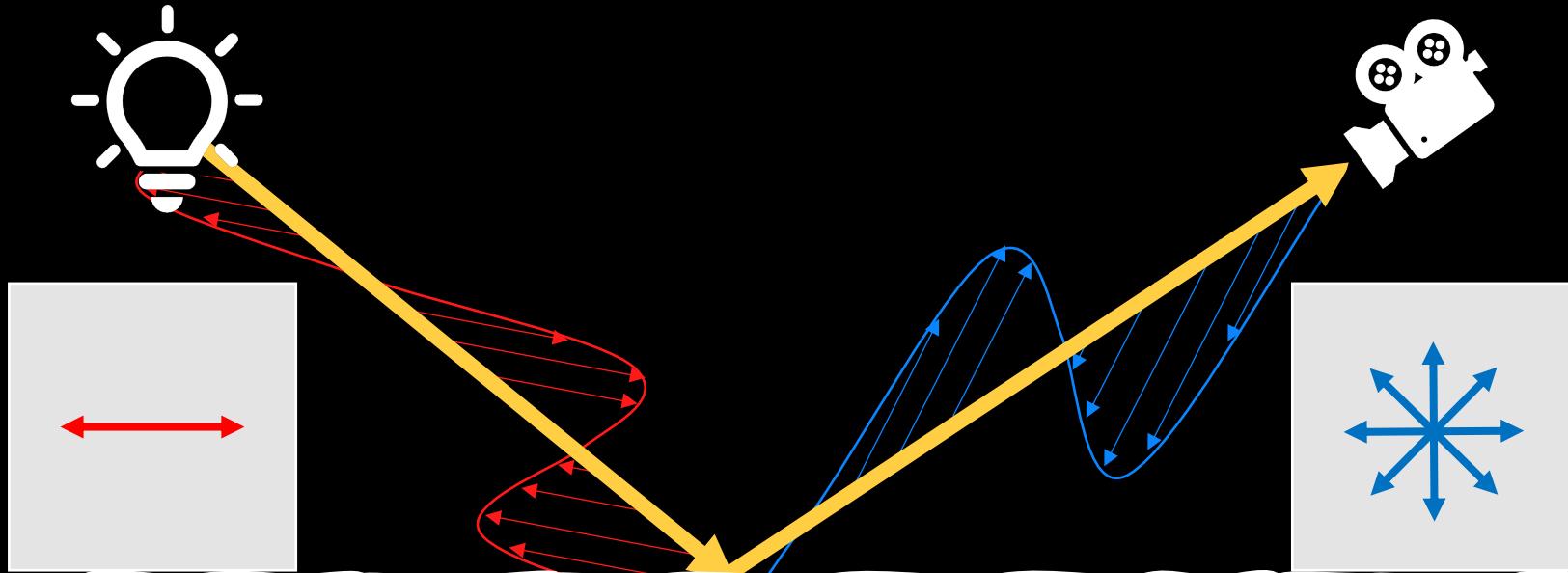
# Polarization changes by reflection



Ideal mirror

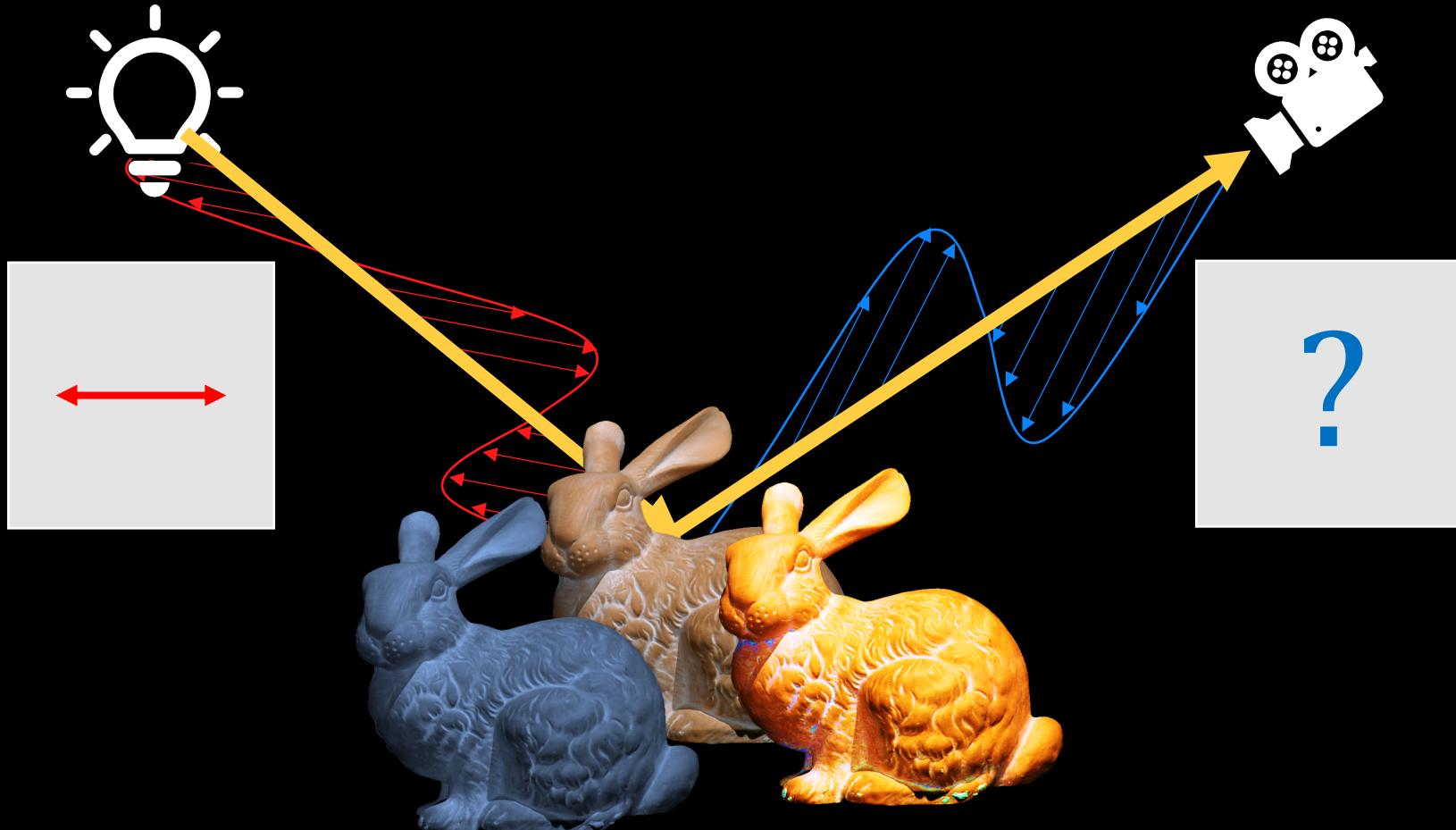
Fresnel reflection

# Polarization changes by reflection



Ideal diffuse surface

# Polarization changes by reflection



Real-world material

# BRDF

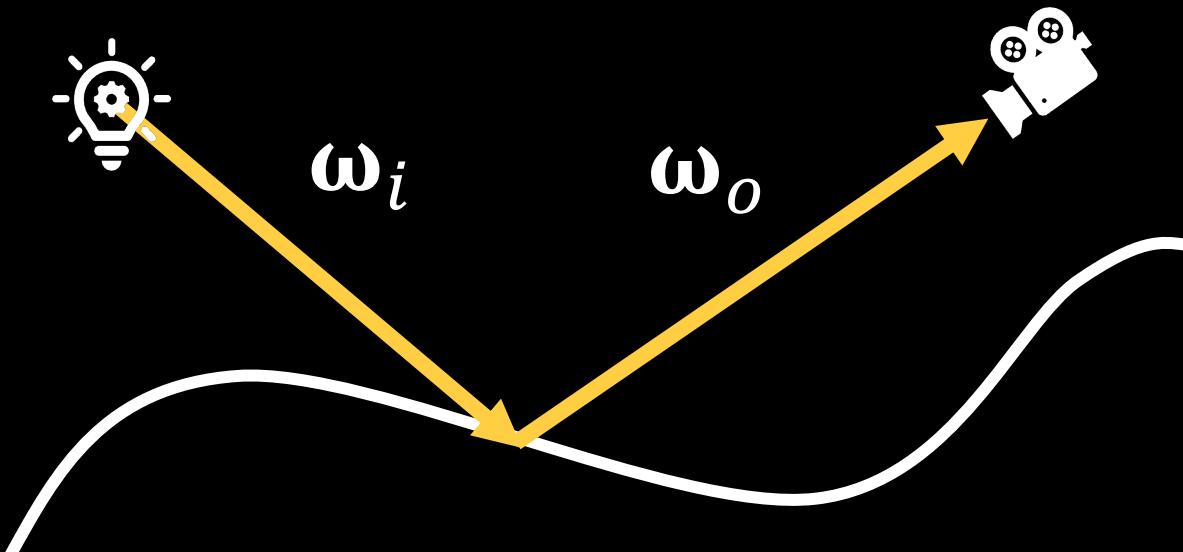
## - *Bidirectional Reflectance Distribution Function*

$$f(\lambda, \omega_i, \omega_o) \in \mathbb{R}^{1 \times 1}$$

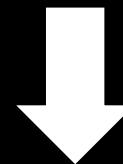
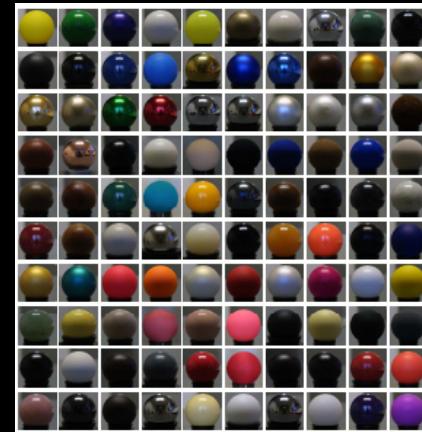
$\omega_i$ : incident light direction

$\omega_o$ : exitant light direction

$\lambda$ : wavelength



Dataset



- Understanding of BRDF
- Analytic modeling
- Forward/inverse rendering

# pBRDF

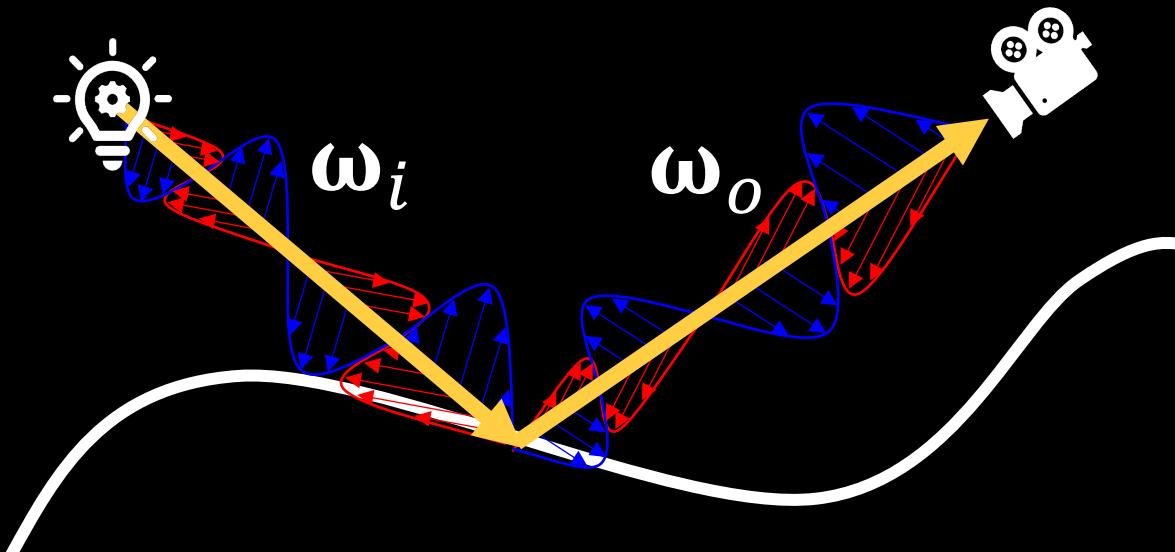
## - *Polarimetric BRDF*

$$\mathbf{M}(\lambda, \omega_i, \omega_o) \in \mathbb{R}^{4 \times 4}$$

$\omega_i$ : incident light direction

$\omega_o$ : exitant light direction

$\lambda$ : wavelength



### Dataset

[Riviere et al.], [Wellems et al.], [Boher et al.]

- Limited directional coverage
- Incomplete polarization change
- A few materials
- Not publicly available



- Understanding of pBRDF
- Analytic modeling
- Forward/inverse rendering

# First comprehensive pBRDF dataset

- large directional coverage
- complete polarization change
- 25 real-world materials



# Acquisition system - design goals

## 1. Direction

full coverage  
for analysis and rendering

## 2. Polarization

complete change of  
polarization

## 3. Spectrum

narrow-spectral band

## 4. Capture time

reasonable amount of capture time

# Solutions

Image-based acquisition  
[Matusik et al. 03]

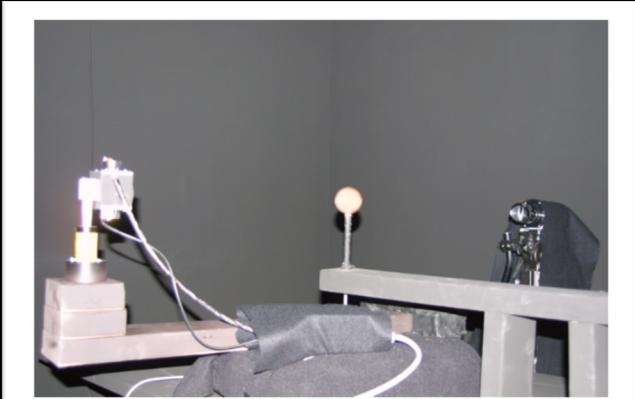
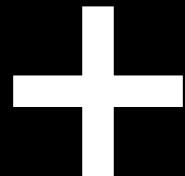


Figure 2: A photograph of our high-speed BRDF measurement gantry.



Spectroscopic ellipsometry  
[Azzam et al. 78]

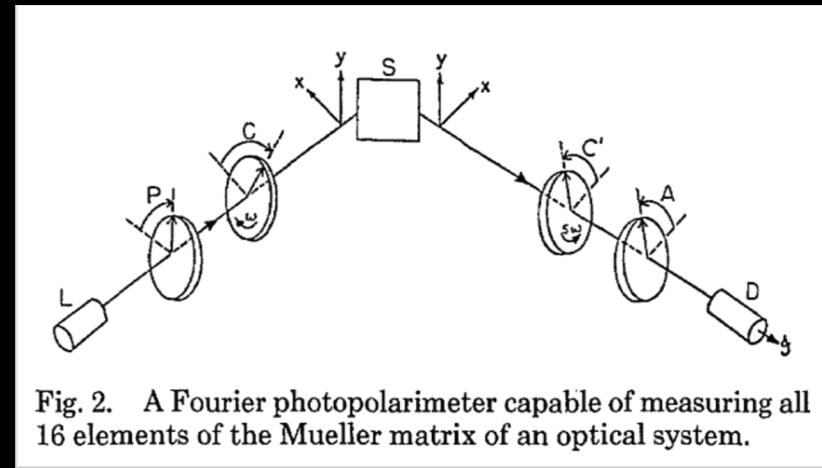
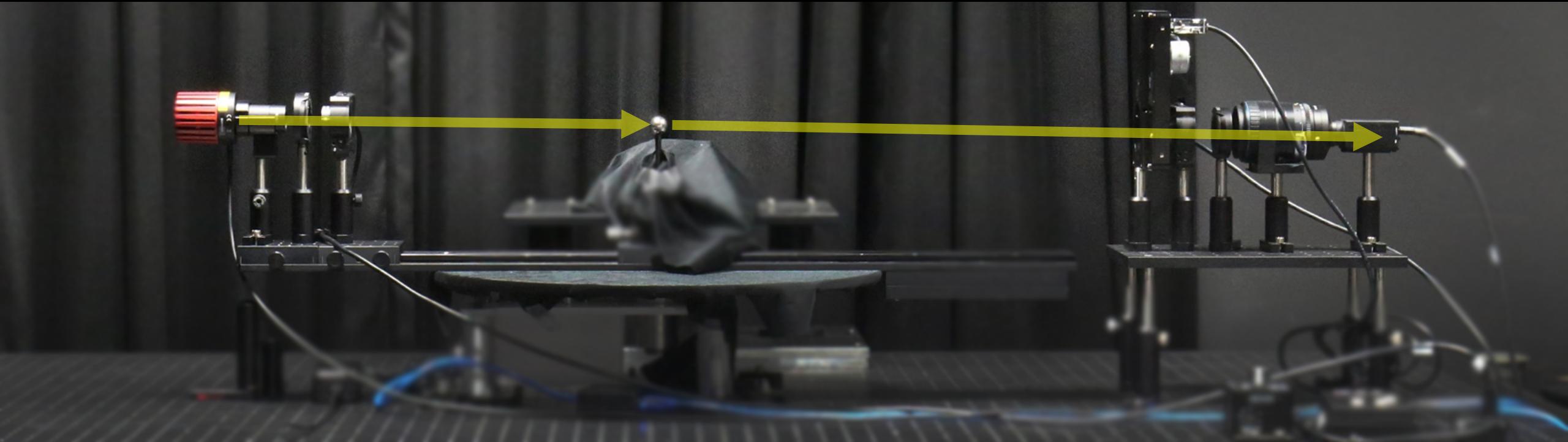


Fig. 2. A Fourier photopolarimeter capable of measuring all 16 elements of the Mueller matrix of an optical system.

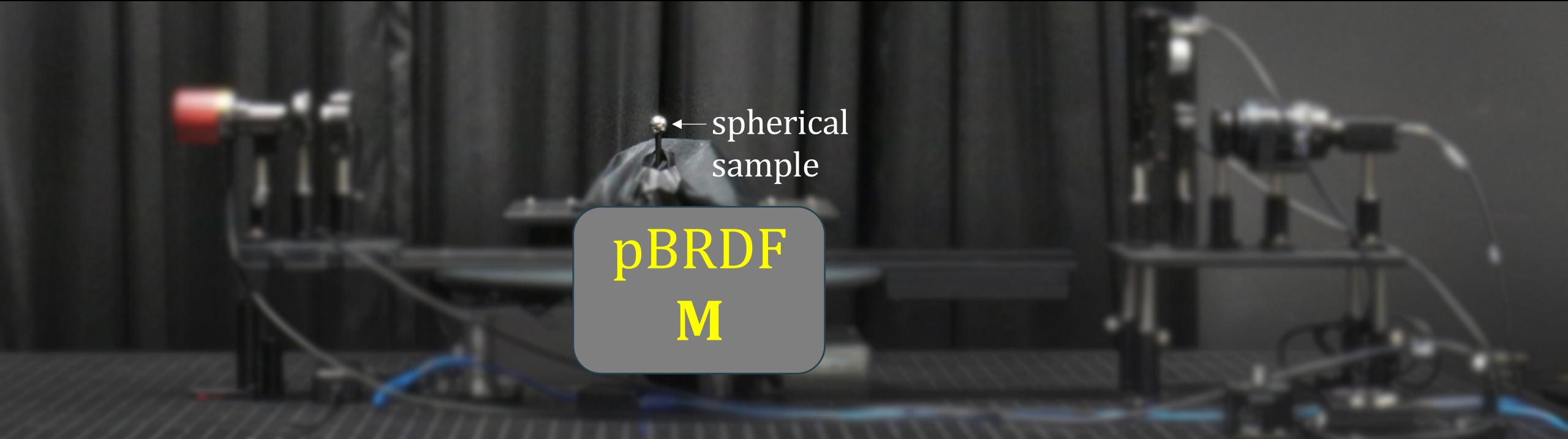
## Capture time

3 days per material

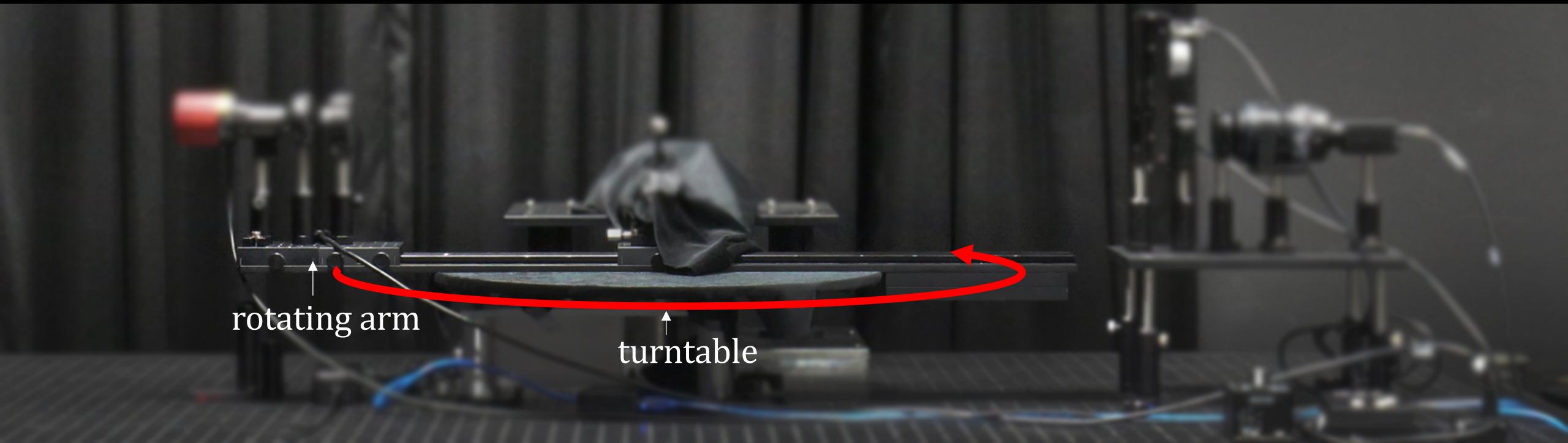
# Our acquisition system



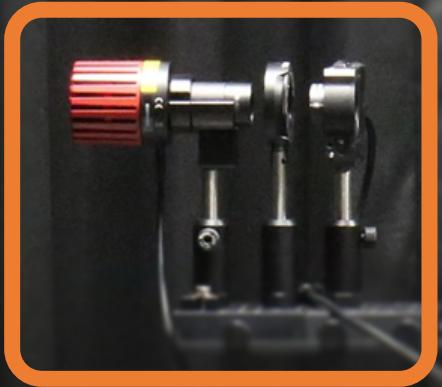
# Homogeneous spherical sample



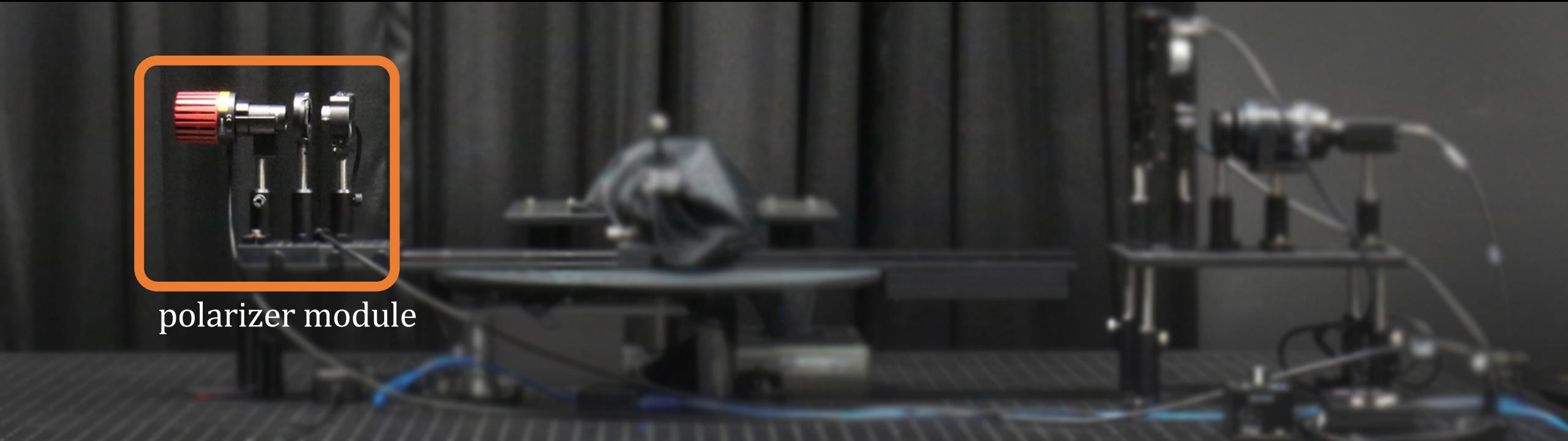
# Turntable



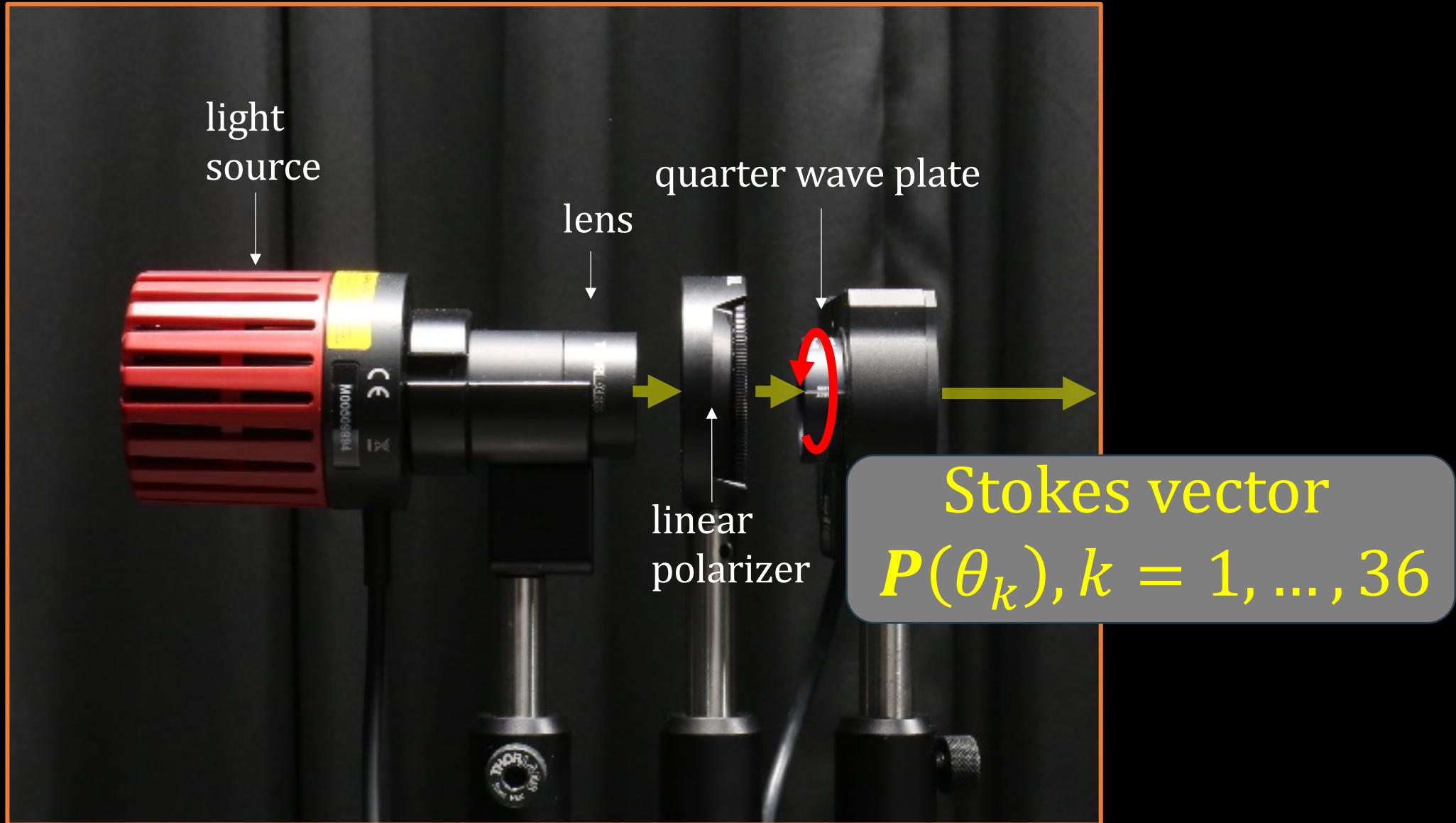
# Polarizer module



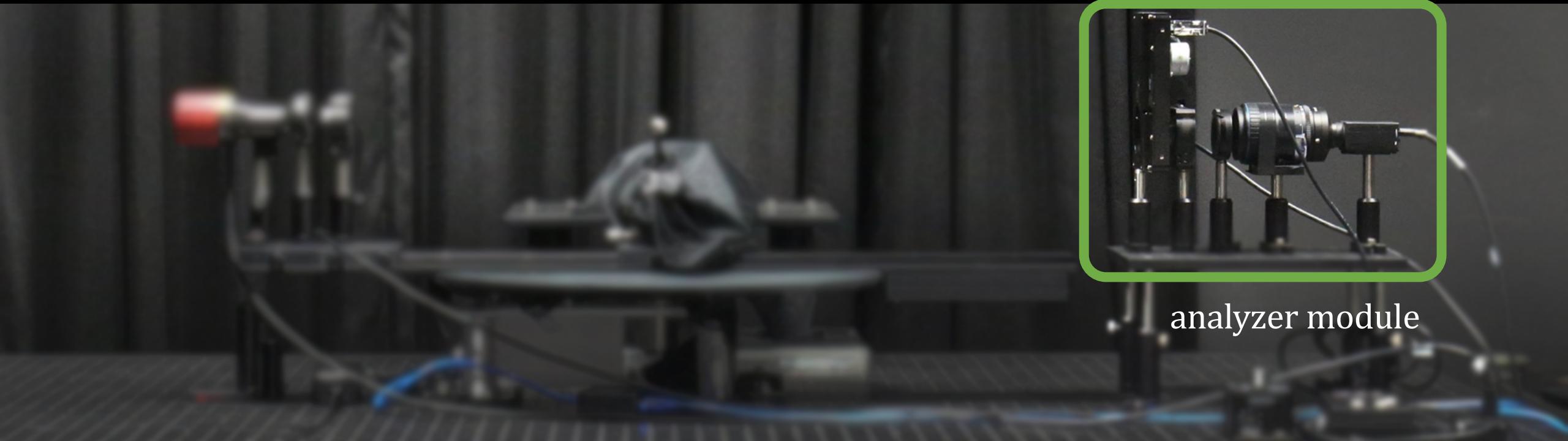
polarizer module



# Polarizer module

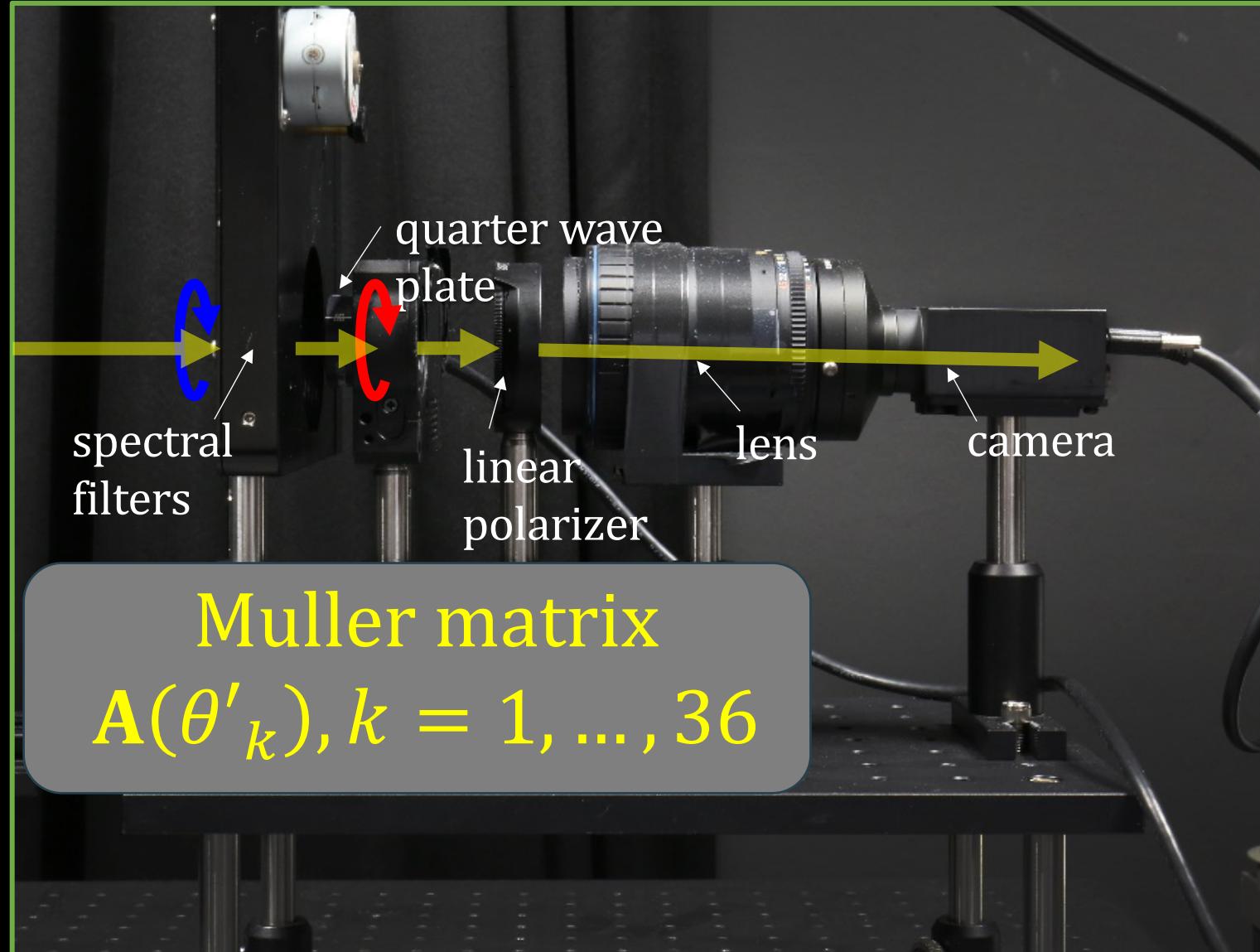
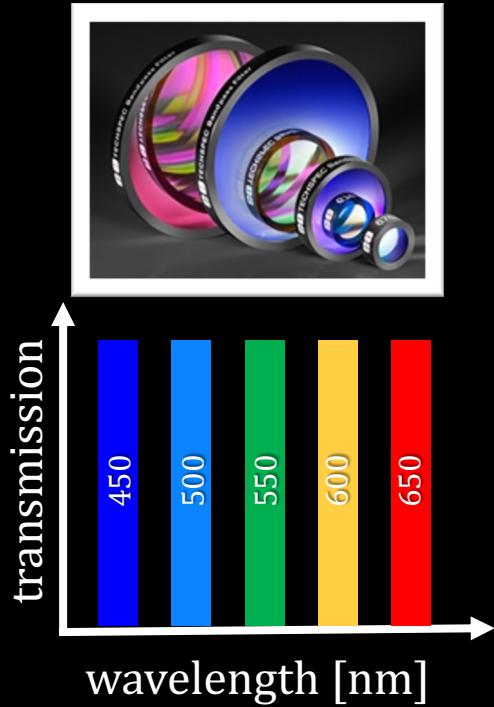


# Analyzer module

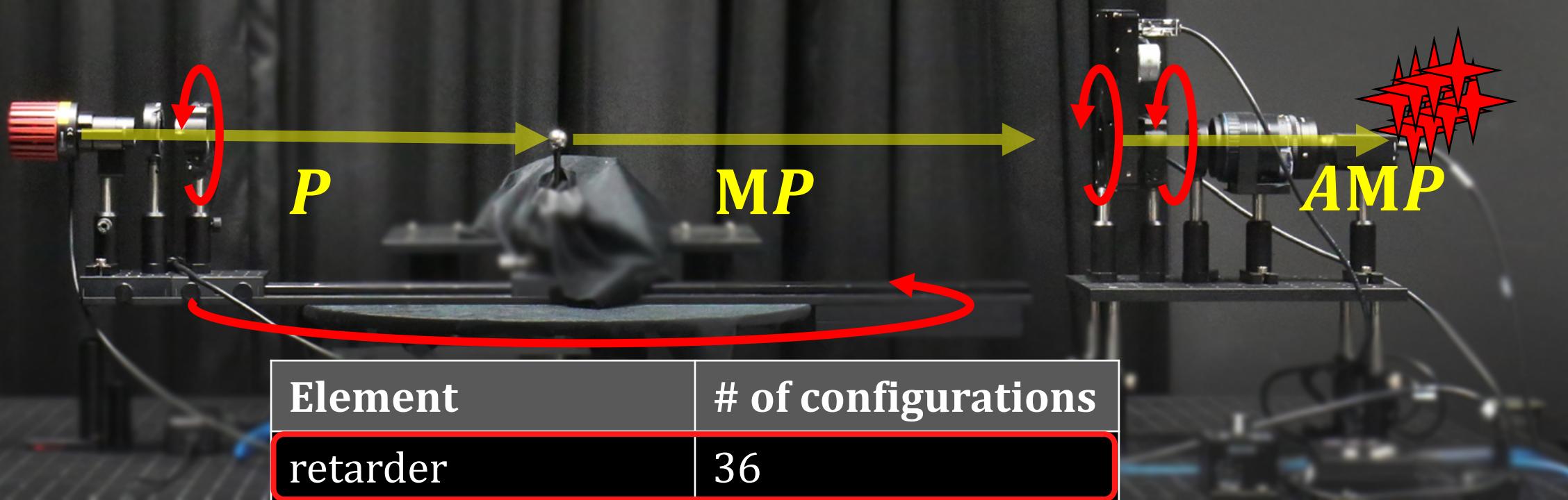


analyzer module

# Analyzer module



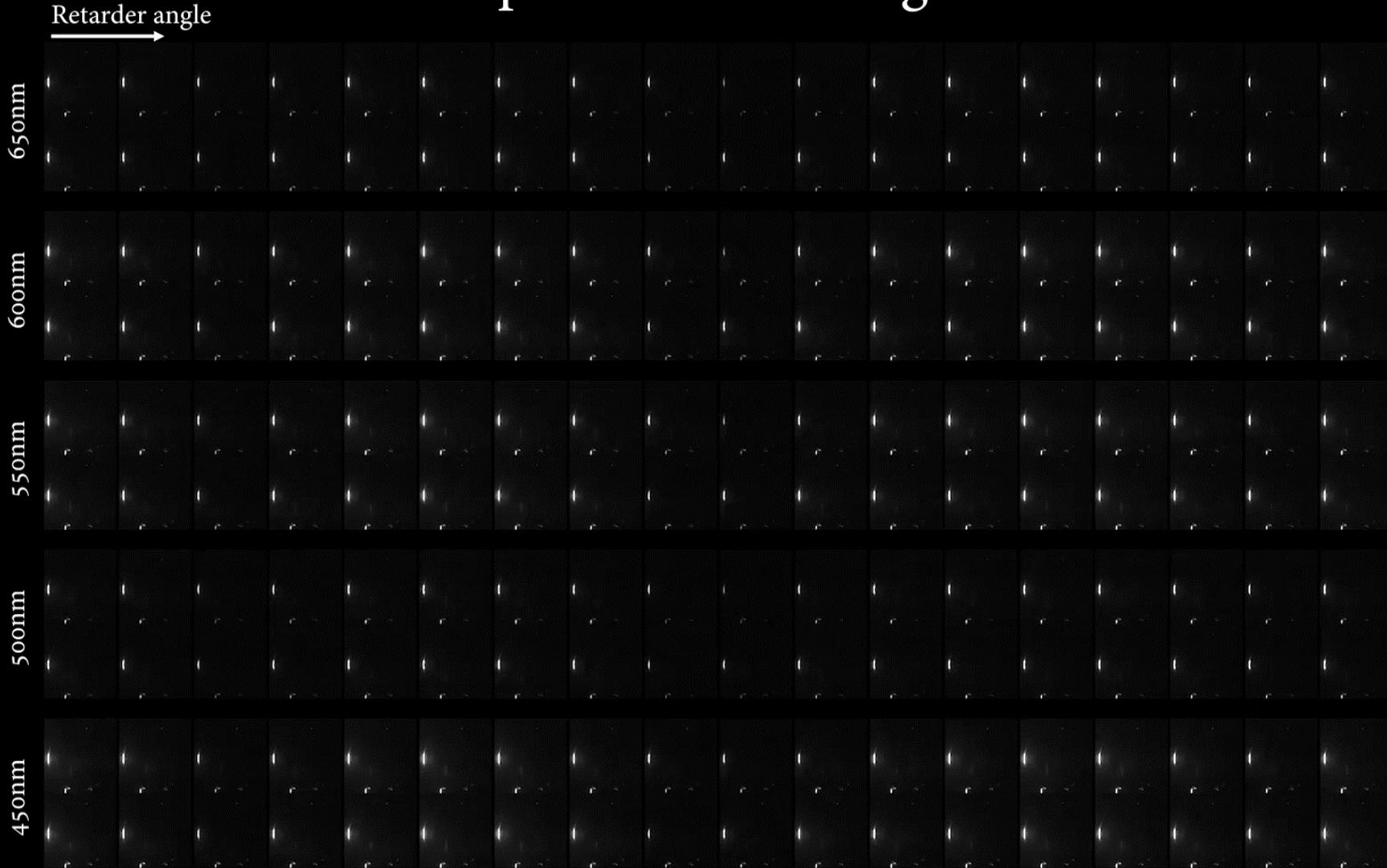
# Multiple configurations



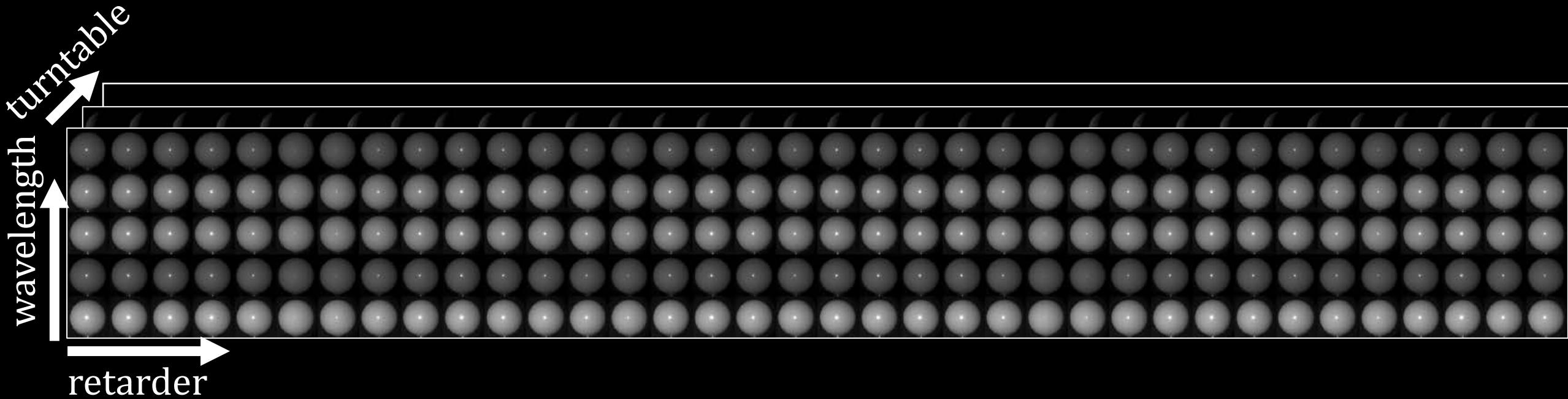
Element	# of configurations
retarder	36
turntable	147
spectral filter	5
exposure	8

# Captured data

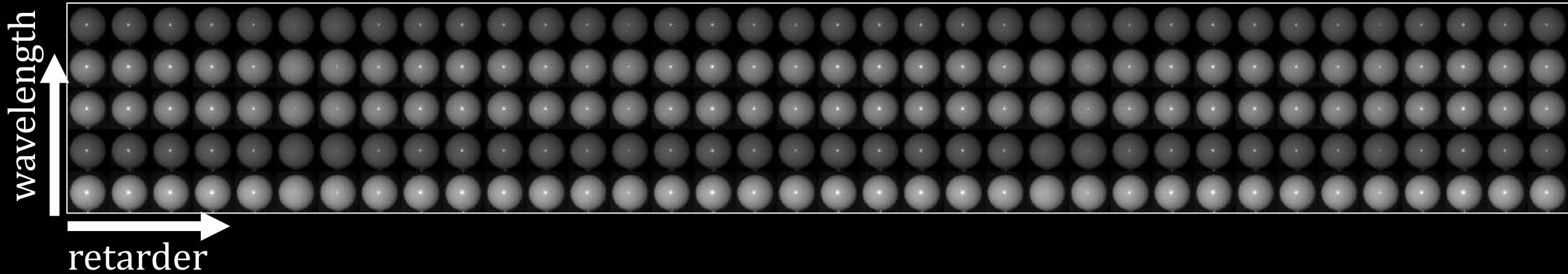
Captured raw data: gold



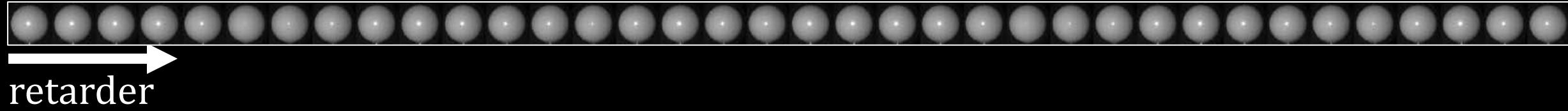
# Captured data to Mueller matrix



For each turntable angle



For each turntable angle, wavelength



For each turntable angle, wavelength, pixel



# Captured data to Mueller matrix

For each turntable angle, wavelength, pixel

$$\begin{array}{c} \text{captured} \\ \downarrow \\ f(\theta_k) \end{array}$$

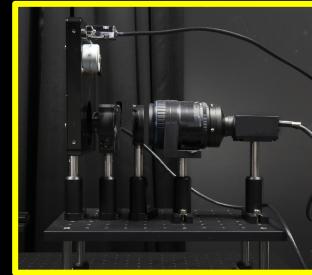


\* known  
\* unknown

# Captured data to Mueller matrix

For each turntable angle, wavelength, pixel

$$\begin{array}{ccc} \text{captured} & & \text{analyzing optics} \\ \downarrow & & \downarrow \\ f(\theta_k) & & A(\theta' k) \end{array}$$



\* known

\* unknown

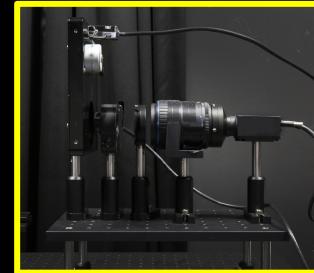
# Captured data to Mueller matrix

For each turntable angle, wavelength, pixel

captured  
↓  
 $f(\theta_k)$



analyzing optics  
↓  
 $A(\theta' k)$



polarizing optics  
↓  
 $P(\theta_k)$

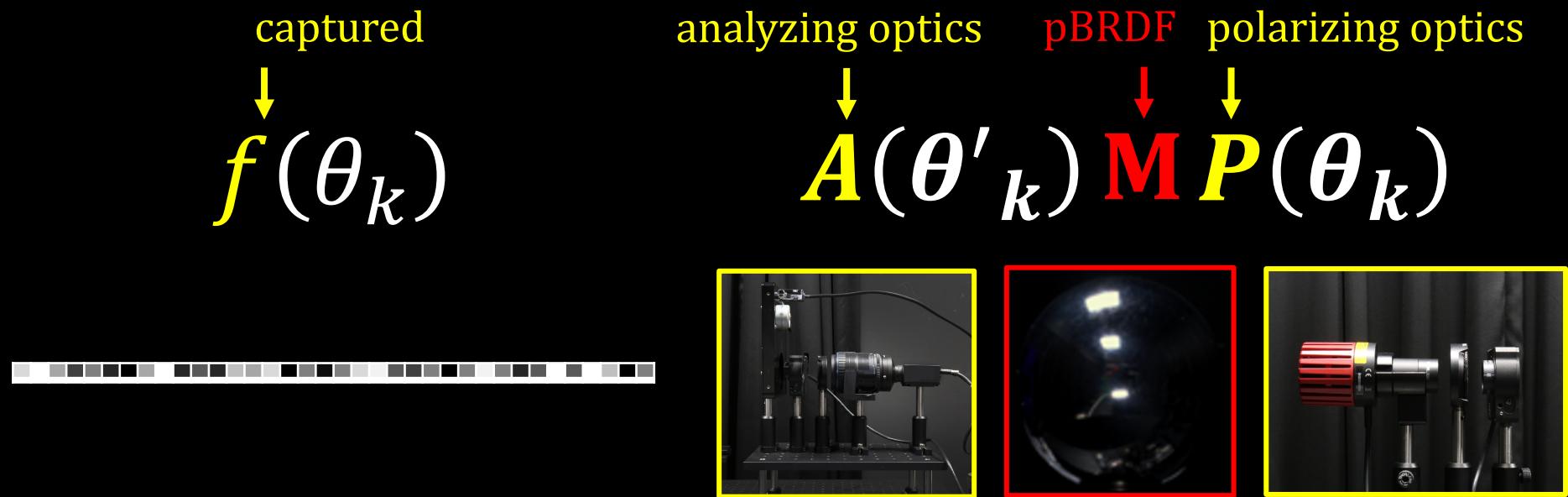


\* known

\* unknown

# Captured data to Mueller matrix

For each turntable angle, wavelength, pixel



\* known

\* unknown

# Captured data to Mueller matrix

For each turntable angle, wavelength, pixel

$$\text{minimize}_{\mathbf{M}} \sum_{k=1}^{36} \{ f(\theta_k) - [A(\theta'_k) \mathbf{M} P(\theta_k)]_0 \}^2$$

captured      analyzing optics      pBRDF      polarizing optics



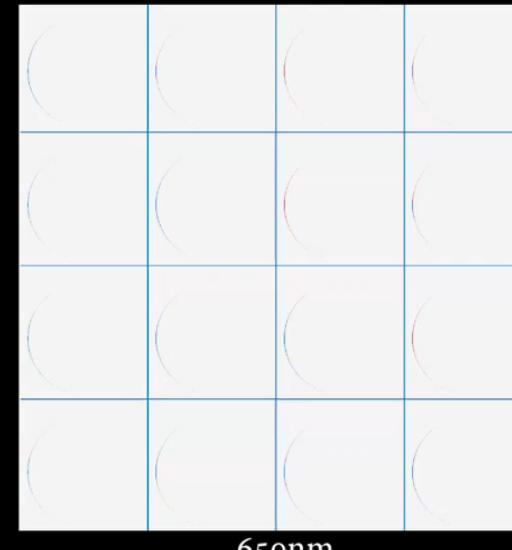
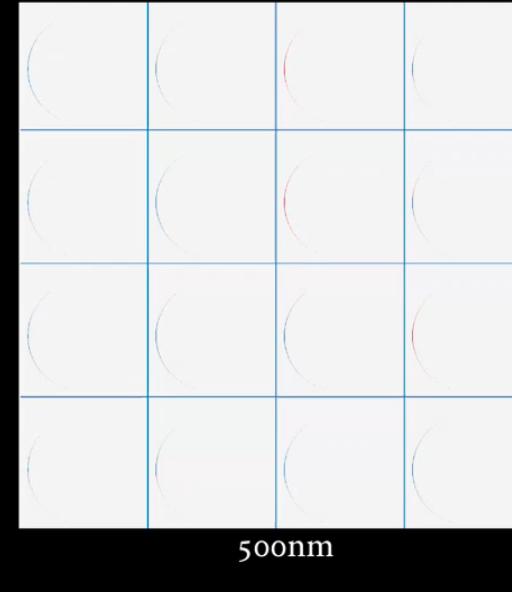
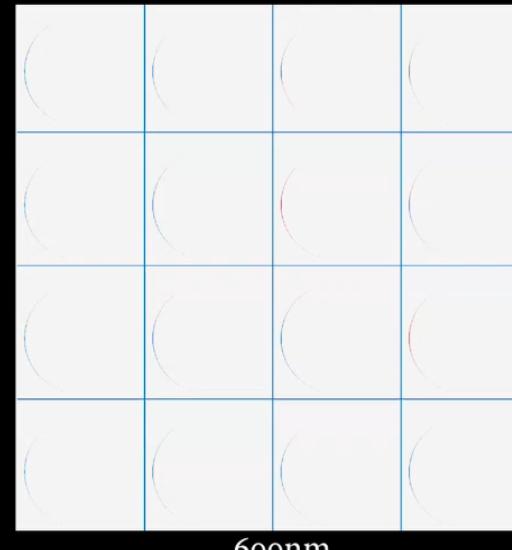
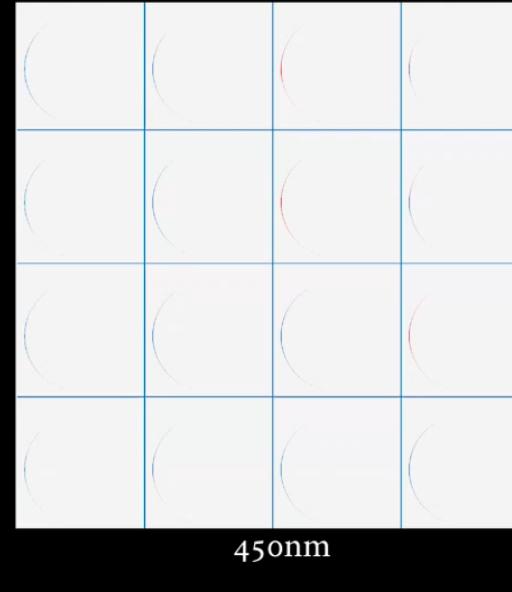
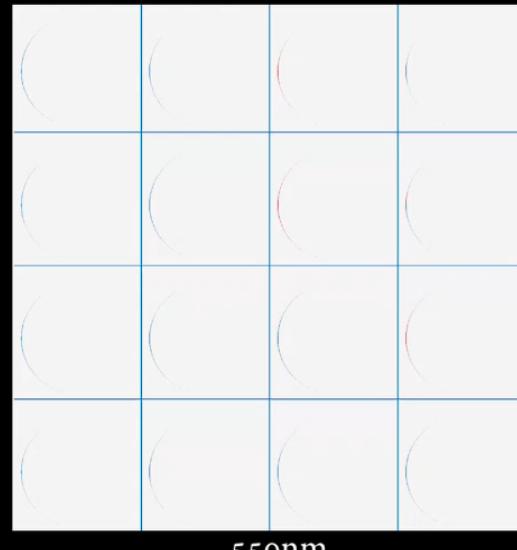
\* known

\* unknown

# Reconstructed per-pixel pBRDF

Reconstructed  
per-pixel pBRDF:  
gold

Mueller matrix value



# pBRDF dataset

$$\mathbf{M}(\lambda, \theta_h, \theta_d, \phi_d)$$

Wavelength 

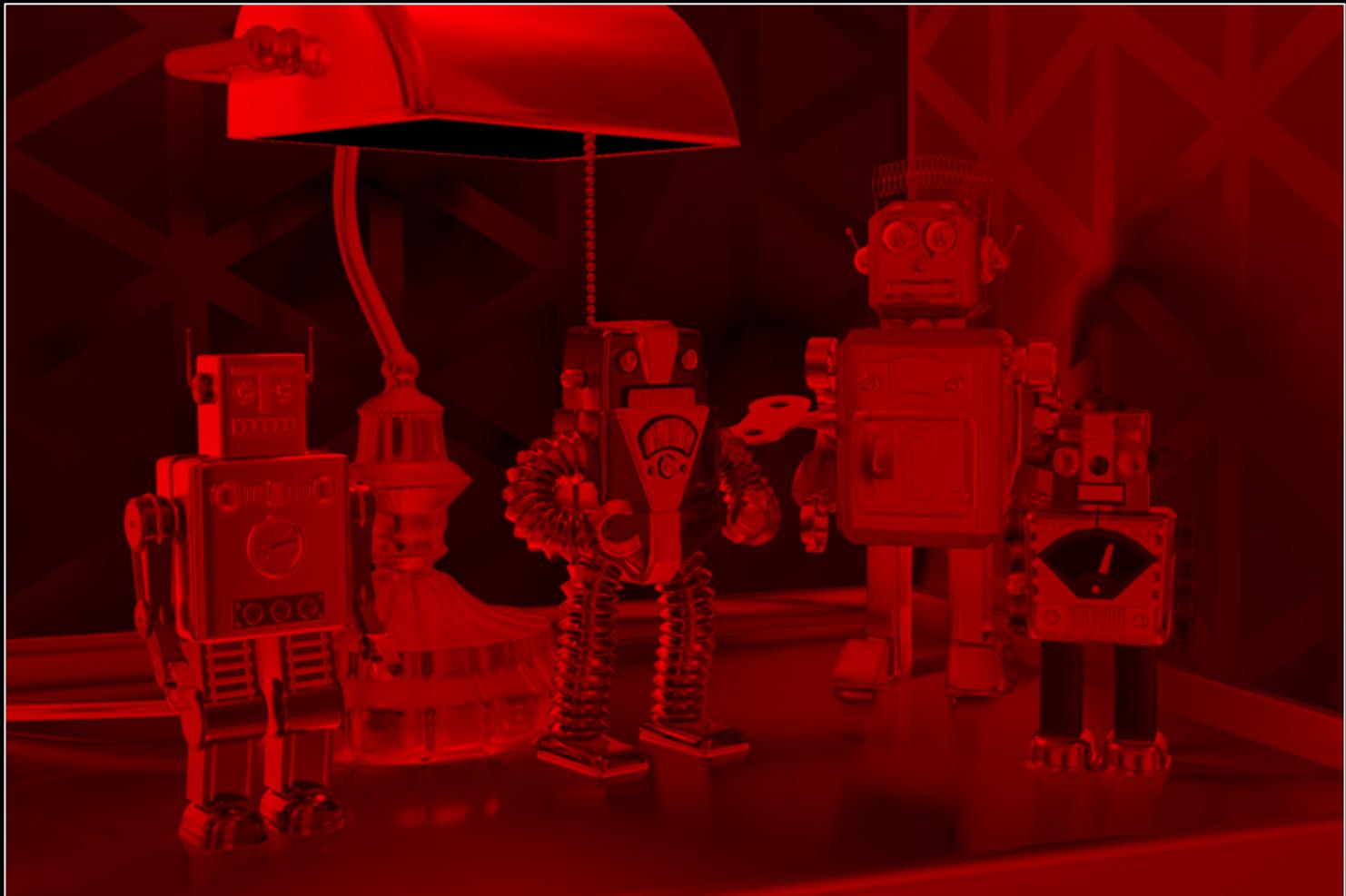
Rusinkiewicz angles 



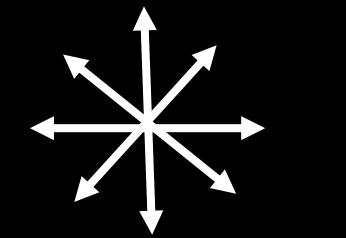
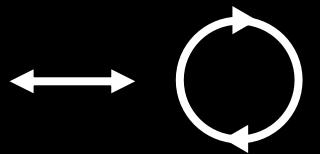
# Intensity rendering



# Degree of polarization (DoP)

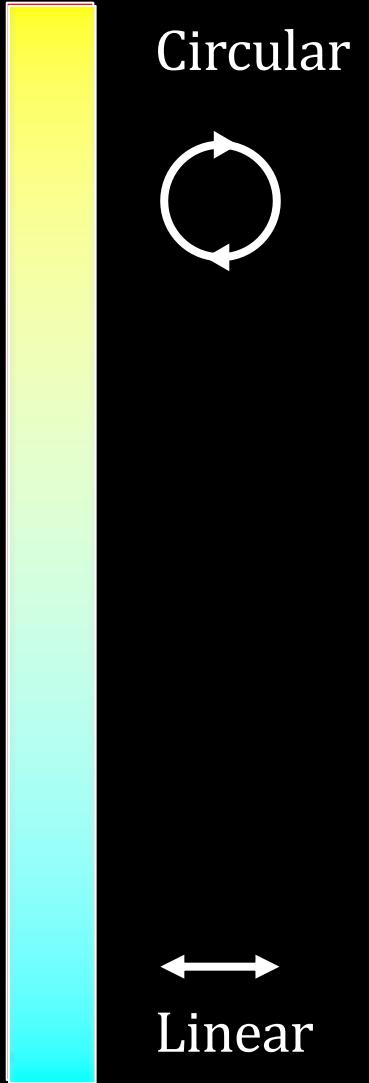
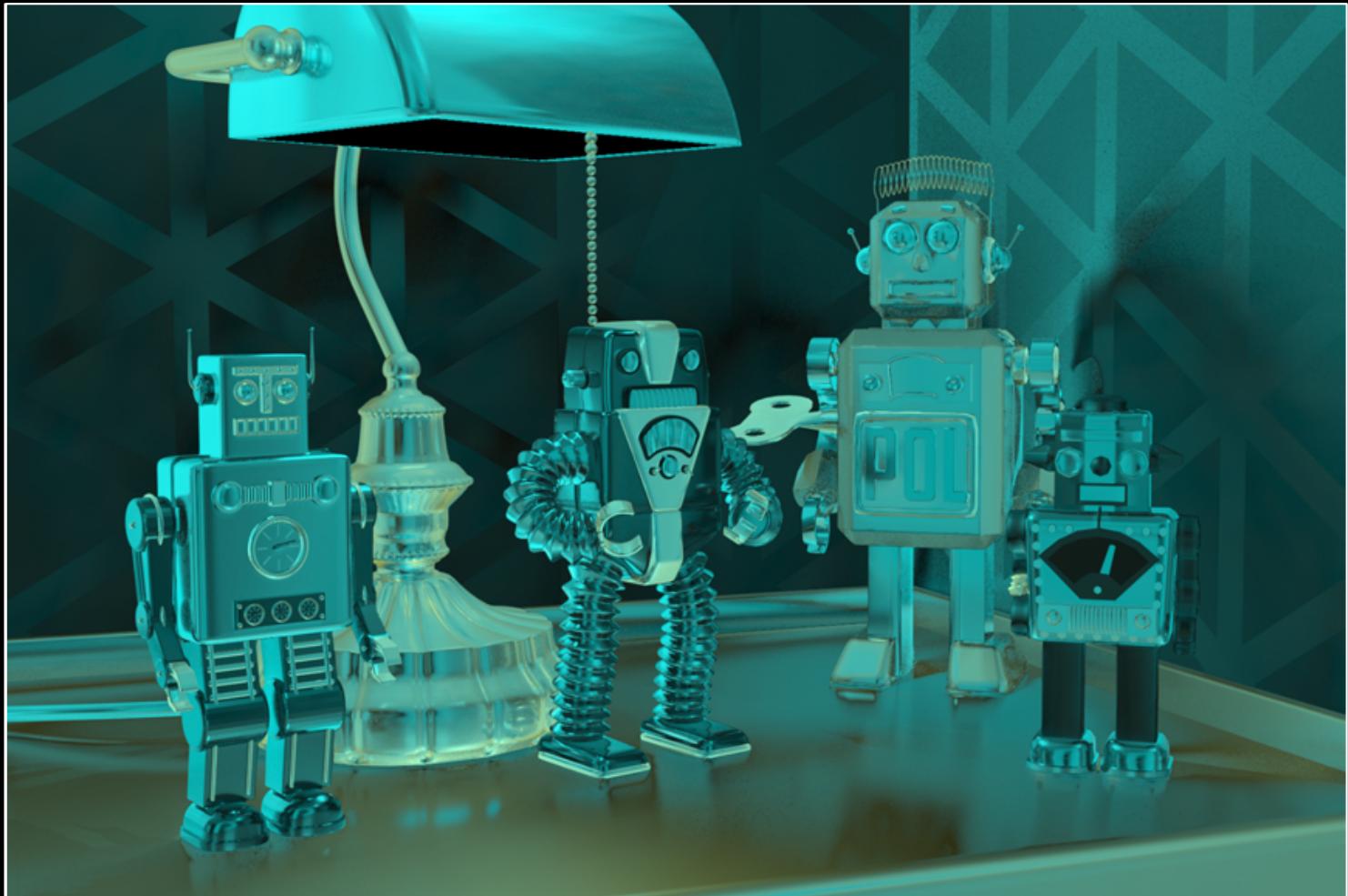


Fully  
polarized

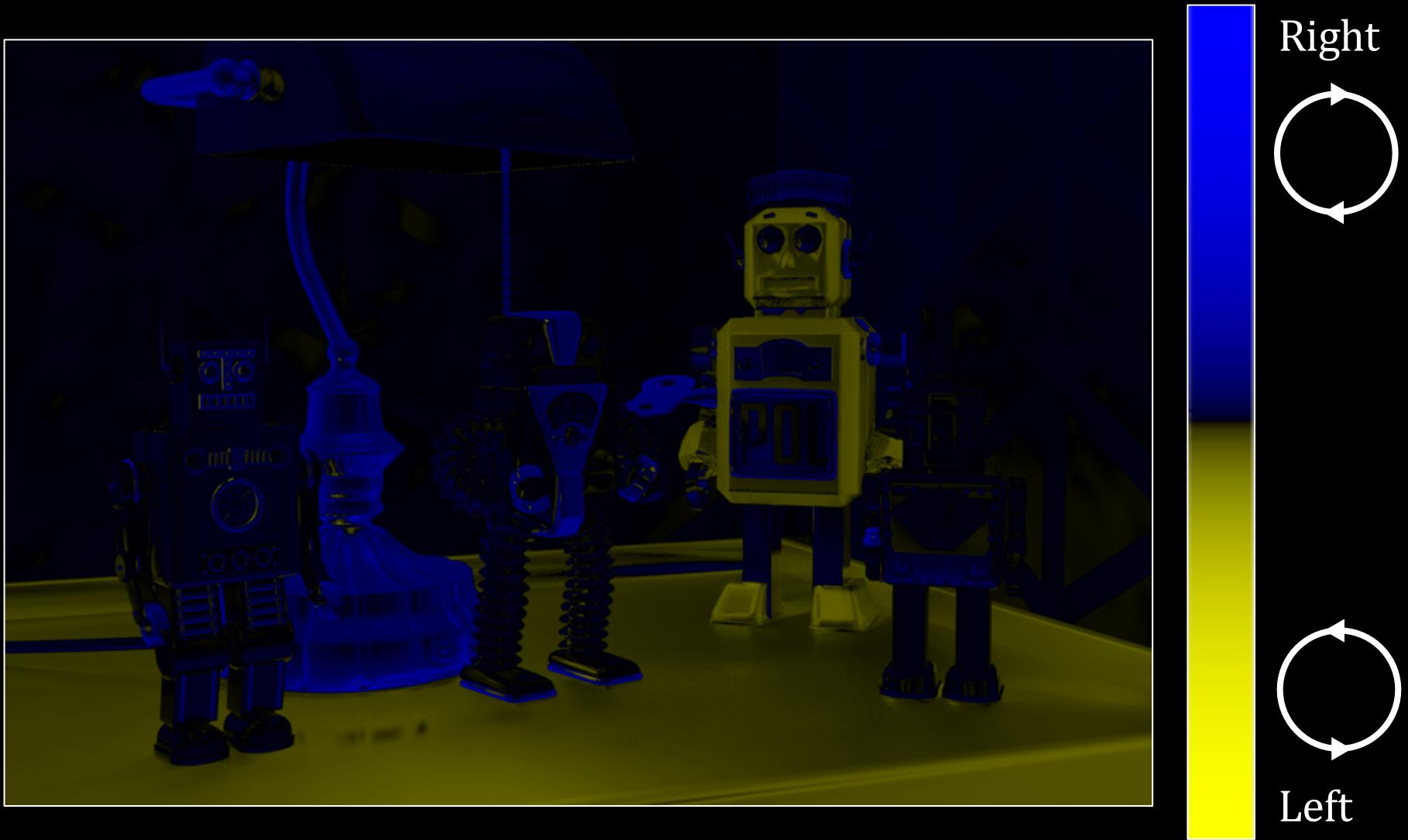


Unpolarized

# Type of polarization (ToP)



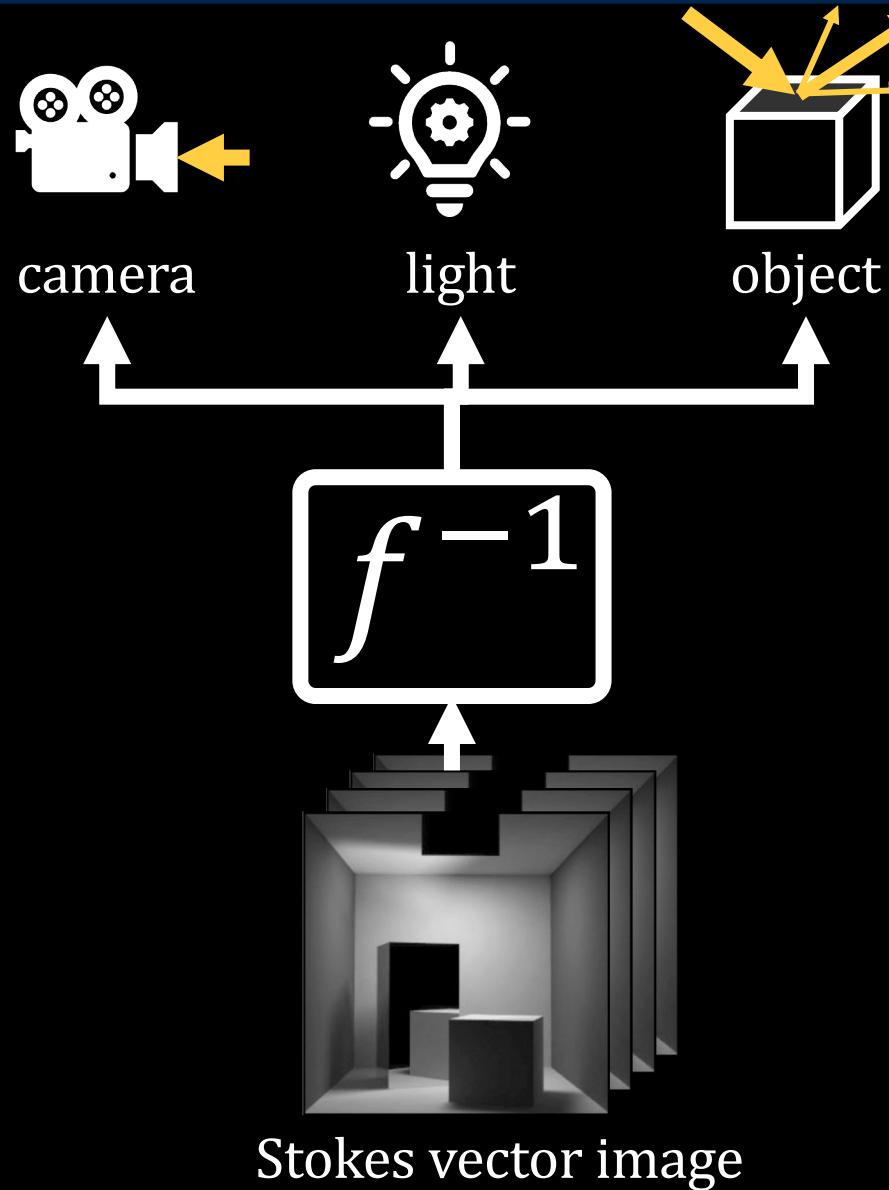
# Chirality of polarization (CoP)



# Angle of linear polarization (AoLP)



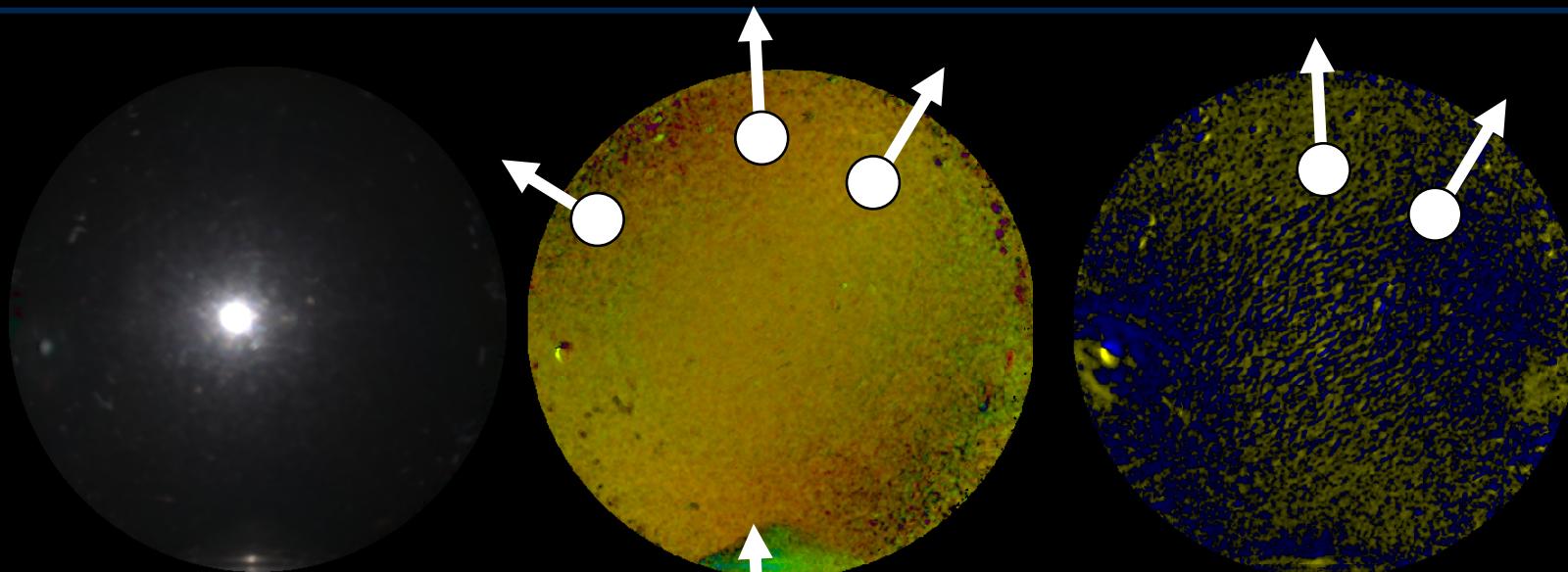
# Polarimetric inverse rendering



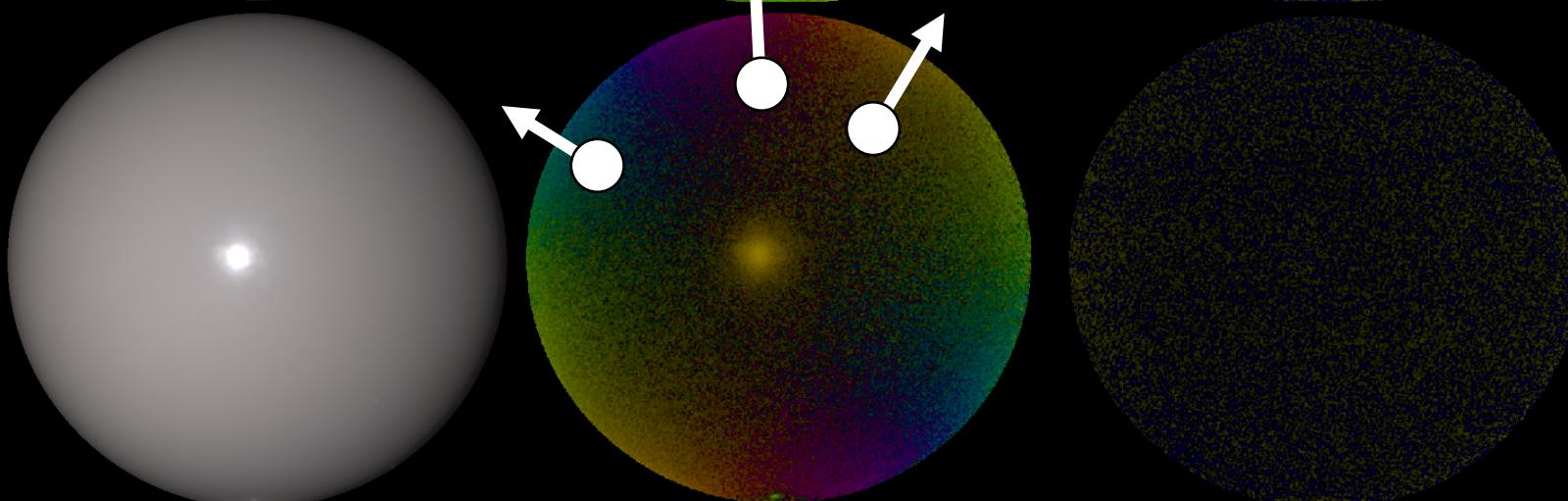
- Surface normals
- Roughness
- Dielectric/metallic
- Color

# Surface normal vs. polarization

Chrome



White billiard



Intensity

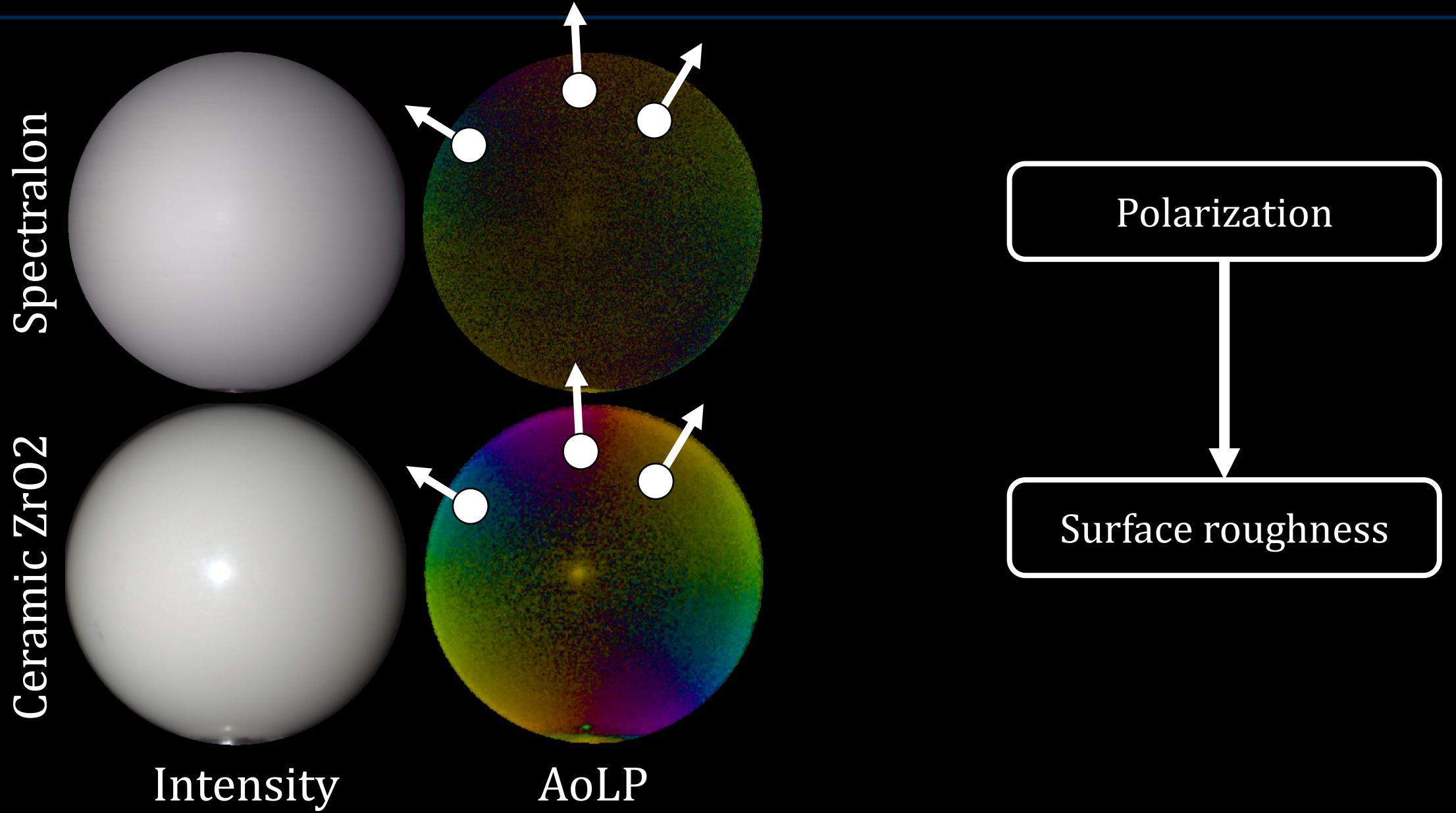
AoLP

CoP

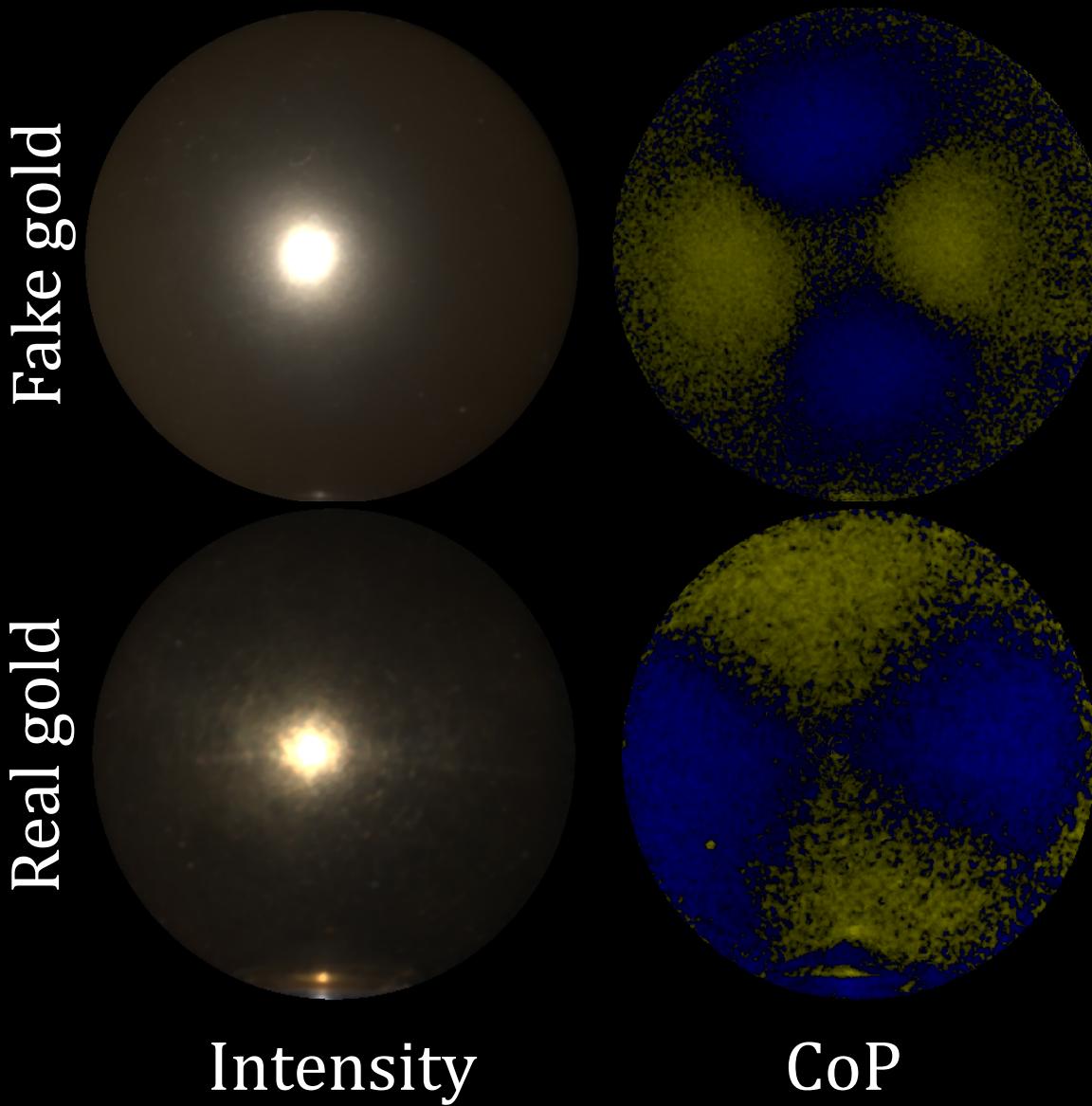
Circular polarization

Surface normals of  
metallic material

# Roughness vs. polarization



# Dielectric/metallic vs. polarization



Polarization

Material type

# Conclusions

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## Contributions

- practical pBRDF acquisition system
- pBRDF dataset
- polarimetric forward and inverse rendering

## *Dataset and code*

- <http://vclab.kaist.ac.kr/siggraph2020>
- <http://rgl.epfl.ch/publications/Baek2020Image>
- <https://www.mitsuba-renderer.org>